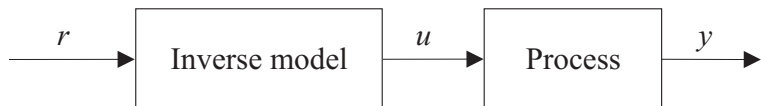


Considered Settings

- Fuzzy or neural model of the process available
(many of the presented techniques apply to other types of models as well)
- Based on the model, design a controller (off line)
- Use the model explicitly within a controller
- Model fixed or adaptive

Inverse Control (Feedforward)



Process model: $y(k+1) = f(\mathbf{x}(k), u(k))$, where

$$\mathbf{x}(k) = [y(k), \dots, y(k - n_y + 1), u(k - 1), \dots, u(k - n_u + 1)]^T$$

Controller: $u(k) = f^{-1}(\mathbf{x}(k), r(k+1))$

When is Inverse-Model Control Applicable?

- ① Process (model) is stable and invertible
- ② The inverse model is stable
- ③ Process model is accurate (enough)
- ④ Little influence of disturbances
- ⑤ In combination with feedback techniques

How to invert $f(\cdot)$?

- 1 Numerically (general solution, but slow):

$$J(u(k)) = \left[r(k+1) - f(\mathbf{x}(k), u(k)) \right]^2$$

minimize w.r.t. $u(k)$

How to invert $f(\cdot)$?

- ① Numerically (general solution, but slow):

$$J(u(k)) = \left[r(k+1) - f(\mathbf{x}(k), u(k)) \right]^2$$

minimize w.r.t. $u(k)$

- ② Analytically (for some special forms of $f(\cdot)$ only):
- affine in $u(k)$
 - singleton fuzzy model

How to invert $f(\cdot)$?

- 1 Numerically (general solution, but slow):

$$J(u(k)) = \left[r(k+1) - f(\mathbf{x}(k), u(k)) \right]^2$$

minimize w.r.t. $u(k)$

- 2 Analytically (for some special forms of $f(\cdot)$ only):
 - affine in $u(k)$
 - singleton fuzzy model
- 3 Construct inverse model directly from data

Inverse of an Affine Model

affine model:

$$y(k+1) = g(\mathbf{x}(k)) + h(\mathbf{x}(k)) \cdot u(k)$$

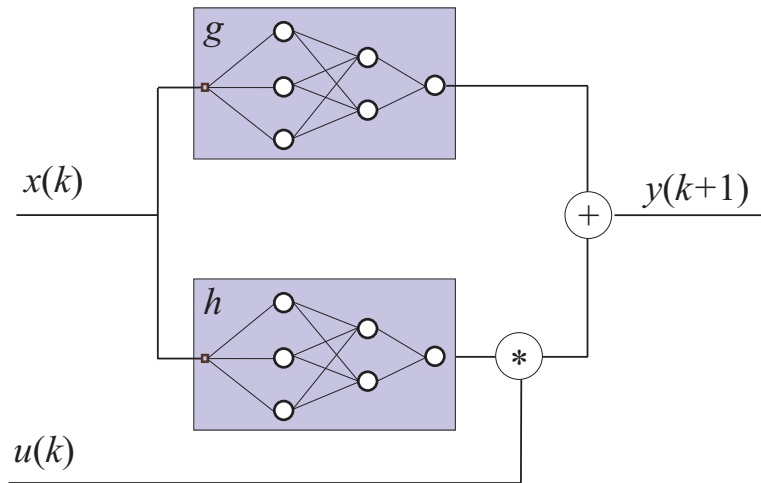
express $u(k)$:

$$u(k) = \frac{y(k+1) - g(\mathbf{x}(k))}{h(\mathbf{x}(k))}$$

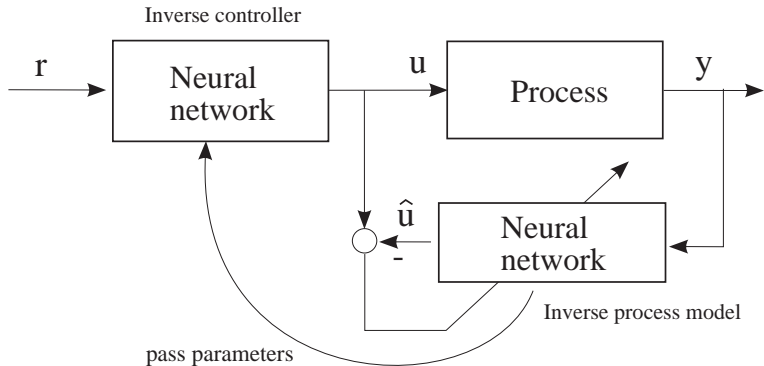
substitute $r(k+1)$ for $y(k+1)$

necessary condition $h(\mathbf{x}) \neq 0$ for all \mathbf{x} of interest

Example: Affine Neural Network



Learning Inverse (Neural) Model



How to obtain \mathbf{x} ?

inverse model: $u(k) = f^{-1}(\mathbf{x}(k), r(k+1))$

- 1 Use the prediction model: $\hat{y}(k+1) = f(\hat{\mathbf{x}}(k), u(k))$

$$\hat{\mathbf{x}}(k) = [\hat{y}(k), \dots, \hat{y}(k - n_y + 1), u(k-1), \dots, u(k - n_u + 1)]^T$$

Open-loop feedforward control

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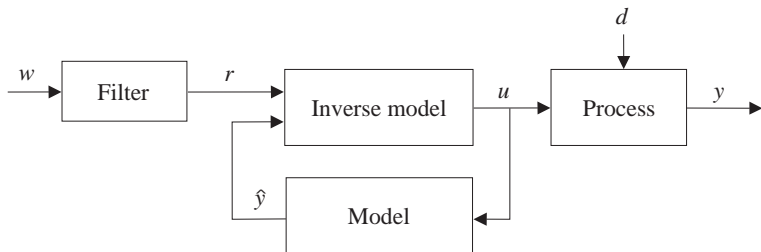
Open-loop feedforward control

- 2 Use measured process output

$$\mathbf{x}(k) = [y(k), \dots, y(k - n_y + 1), u(k-1), \dots, u(k - n_u + 1)]^T$$

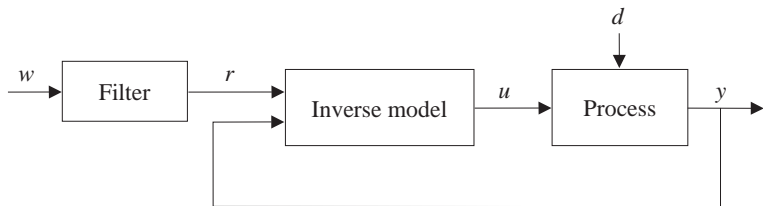
Open-loop feedback control

Open-Loop Feedforward Control



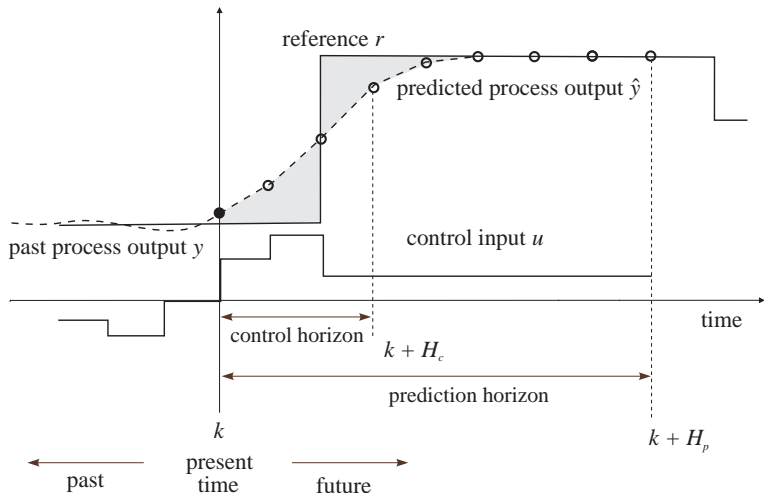
- Always stable (for stable processes)
- No way to compensate for disturbances

Open-Loop Feedback Control



- Can to some degree compensate disturbances
- Can become unstable

Model-Based Predictive Control



Objective Function and Constraints

$$J = \sum_{i=1}^{H_p} \|\mathbf{r}(k+i) - \hat{\mathbf{y}}(k+i)\|_{P_i}^2 + \sum_{i=1}^{H_c} \|\mathbf{u}(k+i-1)\|_{Q_i}^2$$

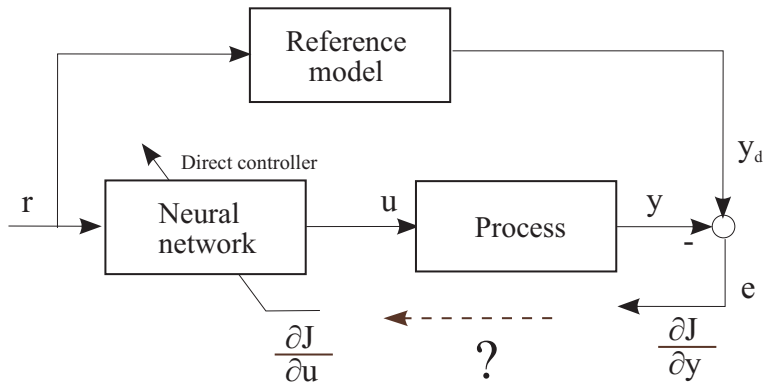
$$\hat{\mathbf{y}}(k+1) = f(\hat{\mathbf{x}}(k), \mathbf{u}(k))$$

$$\begin{array}{ccccc} \mathbf{u}^{\min} & \leq & \mathbf{u} & \leq & \mathbf{u}^{\max} \\ \Delta \mathbf{u}^{\min} & \leq & \Delta \mathbf{u} & \leq & \Delta \mathbf{u}^{\max} \\ \mathbf{y}^{\min} & \leq & \mathbf{y} & \leq & \mathbf{y}^{\max} \\ \Delta \mathbf{y}^{\min} & \leq & \Delta \mathbf{y} & \leq & \Delta \mathbf{y}^{\max} \end{array}$$

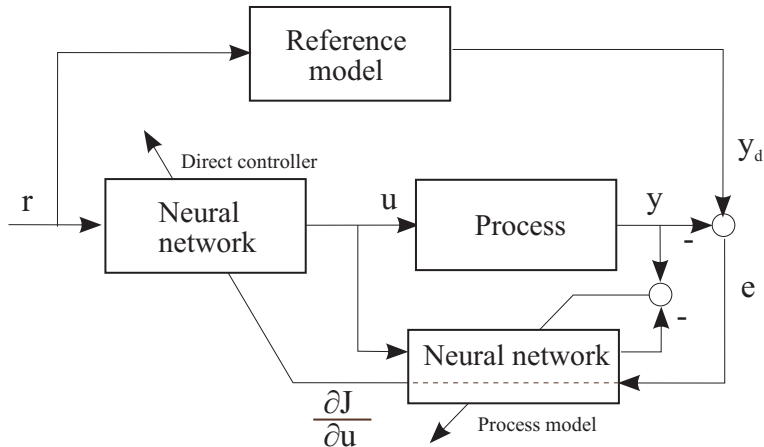
Adaptive Control

- Model-based techniques (use explicit process model):
 - model reference control through backpropagation
 - indirect adaptive control
- Model-free techniques (no explicit model used)
 - reinforcement learning

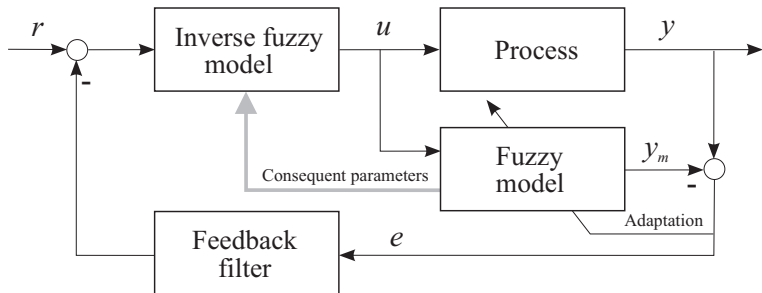
Model Reference Adaptive Neurocontrol



Model Reference Adaptive Neurocontrol



Indirect Adaptive Control



not only for fuzzy models, but also for affine NNs, etc.