

Environmental Sustainability in Control Systems

Design choices, energy use and CO₂e in the use phase
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Intended Learning Outcomes

- Explain how control design impacts energy, resources and emissions.
- Define system boundaries and functional units for fair comparisons.
- Select and report energy and quality metrics together.
- Quantify energy and CO₂e with transparent assumptions.
- Compare controllers via sampling trade-off and Pareto views.

Why Sustainability in Control?

- Control decisions (sampling, constraints, supervision) shape actuator duty and computation.
- Small choices accumulate over thousands of hours → large energy impact.
- Goal: efficient, safe, maintainable operation rather than pointwise optimality.
- Typical applications: fans/pumps, thermal batches, autonomous robots, precision systems, HVAC.

System Boundaries & Use-Phase Focus

- Inside: drive, inverter, gearbox, sensors, embedded controller, communications.
- Outside: upstream utilities and central services unless metered.
- Scope: use phase (manufacturing/EoL excluded unless stated).
- Multiple duty profiles? Evaluate separately and report weighted average.

Functional Units & Normalisation

- Report energy per functional unit (U): per cycle, per tonne, per km, per m³.
- Avoid per-hour unless task value is fixed; otherwise state window and task.
- Example: “0.23 kWh per cycle (± 0.02 kWh).”

Metrics & Reporting

- Primary: energy per U; peak/average power; duty; saturations; starts/stops.
- Quality: settling time, overshoot, RMSE, constraint violations, throughput.
- Emissions: $m_{\text{CO}_2\text{e}} = E(\text{kWh}) \times g$ (state region/year and source).
- Always present energy together with quality and uncertainty.

Methods: Electrical Energy

- Continuous: $E = \int v(t) \cdot i(t) dt$.
- Sampled (rectangle): $E \approx \sum v[k] \cdot i[k] \cdot \Delta t$.
- Sampled (trapezoidal): $E \approx \sum 0.5 \cdot [p[k]+p[k+1]] \cdot \Delta t$, $p[k] = v[k] \cdot i[k]$.
- Convert to kWh: $E(\text{kWh}) = E / (3.6 \times 10^6)$.
- Align timestamps; validate down-sampling.

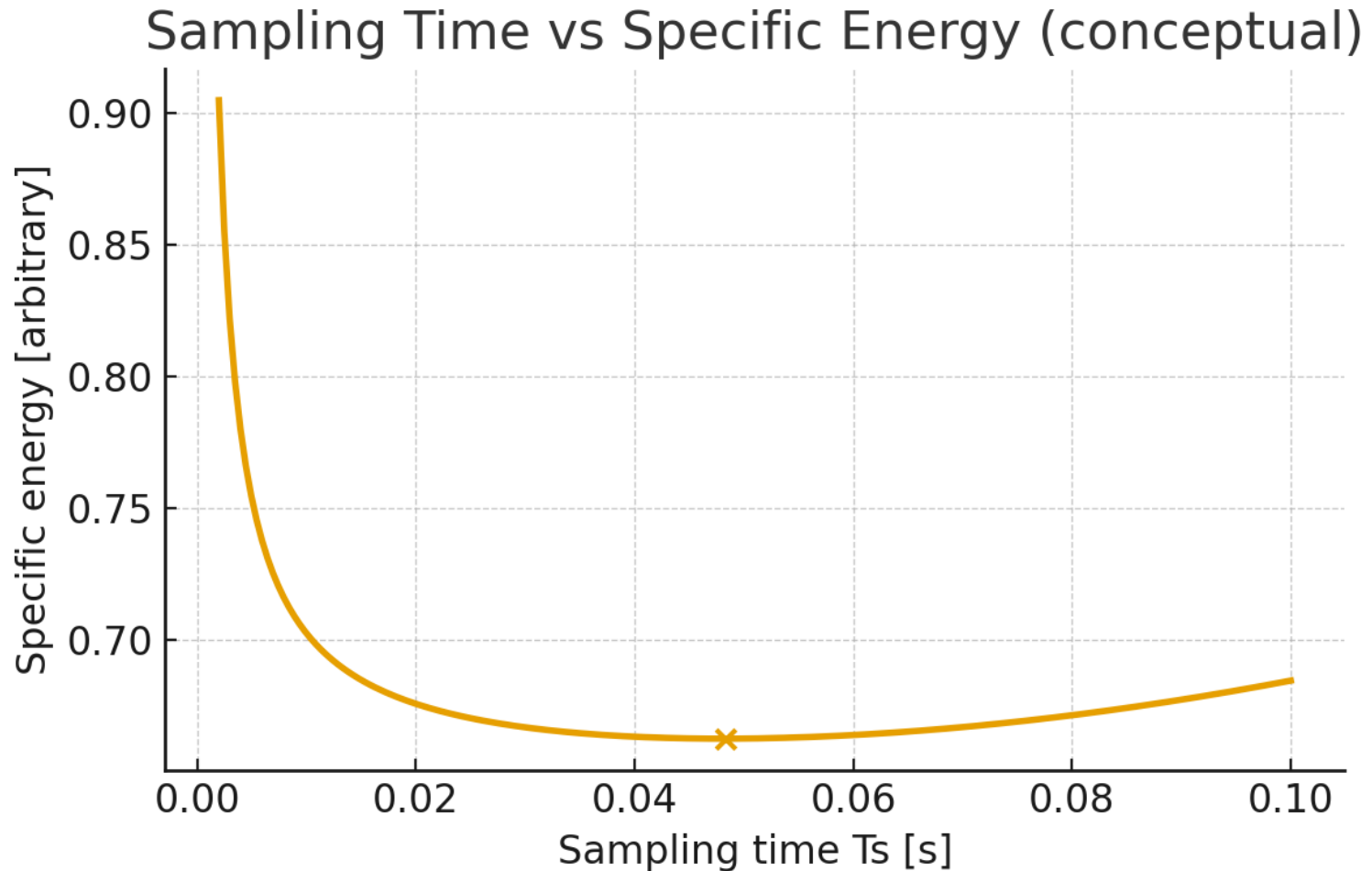
Methods: Emissions & Computation

- Emissions: $m_{\text{CO}_2\text{e}} = E(\text{kWh}) \times g(\text{region/year, units, source})$.
- Compute (proxy): $E_{\text{comp}} \approx P_{\text{idle}} \cdot T + (P_{\text{load}} - P_{\text{idle}}) \cdot u_{\text{CPU}} \cdot T$.
- Duty-factor quick estimate: $D = t_{\text{active}}/T \rightarrow E \approx P_{\text{rated}} \cdot D \cdot T$.
- Include networking/offloaded compute when applicable.

Design Levers: Overview

- Sampling time and anti-windup.
- Set-point shaping and reference governors.
- Constraints (rates/limits) and soft penalties.
- Supervisory switching and scheduling; predictive/adaptive strategies.

Sampling Time vs Specific Energy

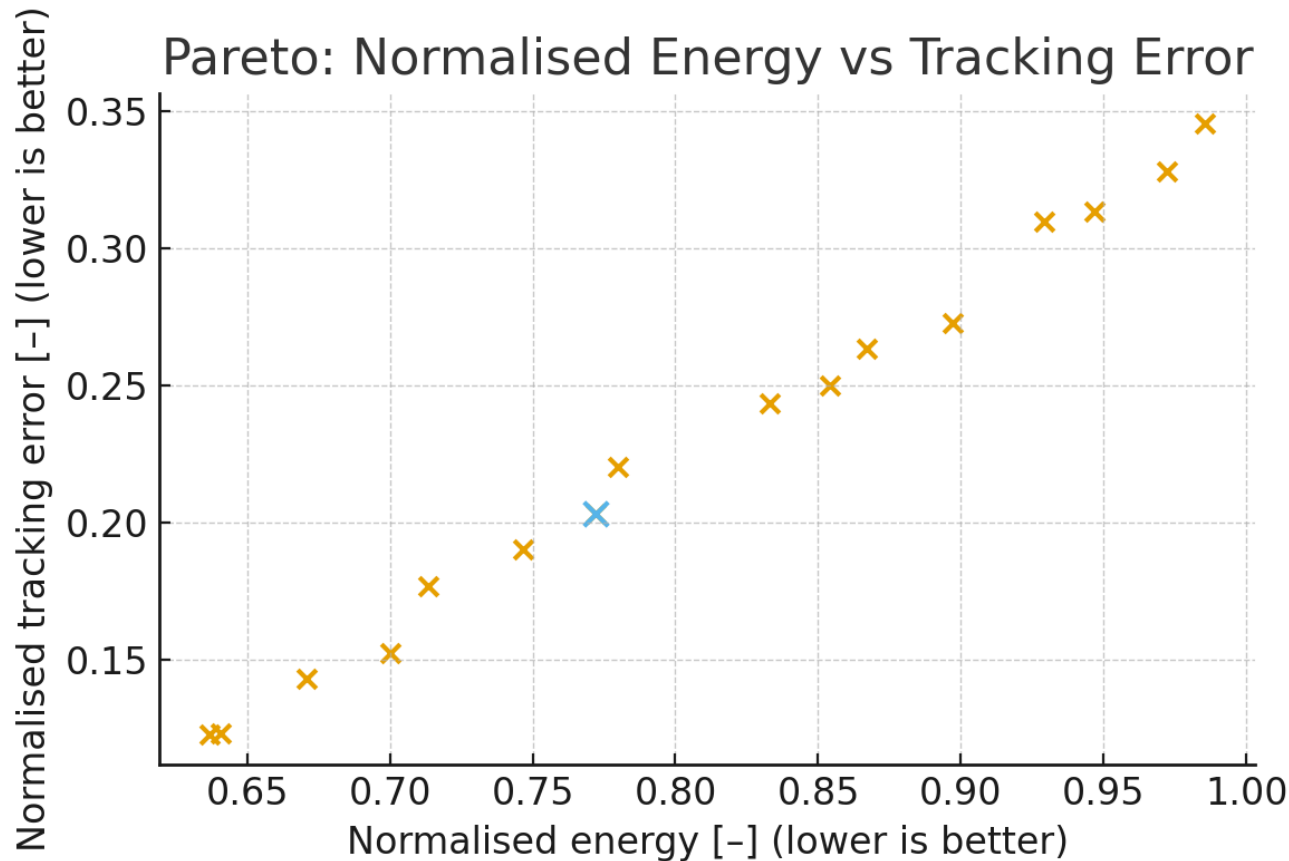


Choose T_s by comparing 2–3 candidates under the same workload.
Target the knee region.

Reading the Sampling Trade-off

- Small T_s \uparrow I/O and CPU overhead.
- Large T_s \downarrow disturbance rejection \rightarrow longer tasks/oscillations.
- Pick near the knee; confirm with measurements.

Pareto: Normalised Energy vs Tracking Error



Same constraints/workload across alternatives.
Prefer points near the knee; add error bars.

Measurement & Logging

- Use true-RMS meters; calibrate and record certificates.
- Synchronise clocks; declare log rates; replicate runs.
- Sanity checks: non-negative energy; plausible peaks; efficiency bracket.

Worked Example: Electrical + CO₂e

- Given $V = 230 \text{ V}$, $I = 2.0 \text{ A}$, $t = 1\,800 \text{ s} \rightarrow E \approx 0.23 \text{ kWh}$.
- With $g = 0.25 \text{ kg CO}_2\text{e/kWh} \rightarrow m_{\text{CO}_2\text{e}} \approx 0.058 \text{ kg per cycle}$.
- Report uncertainty band and the source of g .

Worked Example: Mechanical Proxy

- Given $\tau = 5.0 \text{ N}\cdot\text{m}$, $\omega = 120 \text{ rad/s}$, $T = 60 \text{ s} \rightarrow E_{\text{mech}} \approx 0.01 \text{ kWh}$.
- If $\eta = 0.8 \rightarrow E_{\text{elec}} \approx 0.0125 \text{ kWh}$ (range 0.012–0.014 kWh).
- Mechanical energy is a lower bound unless efficiencies are known.

Mini Case Study: Variable-Speed Pump

- Baseline: abrupt set-points; Alternative: s-curve (4 s) + anti-windup.
- Energy per batch: 0.62 \rightarrow 0.57 kWh (−8%). Peak power: 2.3 \rightarrow 1.9 kW (−17%).
- Overshoot: 12% \rightarrow 4%; constraint violations eliminated.

Summary & Takeaways

- Define boundaries and functional units; document assumptions.
- Tune with energy and robustness in mind (sampling, shaping, wind-up).
- Use Pareto views; choose the knee region.
- Report energy/CO₂e with uncertainty; sustain efficiency with supervision.

Discussion

- Where is your Pareto knee and how sensitive is it?
- Which small change yields the largest saving?
- Which assumptions dominate uncertainty?
- How will supervision/maintenance sustain gains over time?