

# **Automazione (Laboratorio)**

## **Reti Neurali Per L'identificazione, Predizione Ed Il Controllo**

Lecture 1:

Introduction to Neural Networks  
(Machine Learning)

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## **References**

### **Textbook (suggested):**

- *Neural Networks for Identification, Prediction, and Control*, by Duc Truong Pham and Xing Liu. Springer Verlag; (December 1995). ISBN: 3540199594
- *Nonlinear Identification and Control: A Neural Network Approach*, by G. P. Liu. Springer Verlag; (October 2001). ISBN: 1852333421



# Course Overview

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1. Introduction
  - i. Course introduction
  - ii. Introduction to neural network
  - iii. Issues in neural network
2. Simple neural network
  - i. Perceptron
  - ii. Adaline
3. Multilayer Perceptron
  - i. Basics
4. Radial basis networks
5. Application examples

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# Machine Learning

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- Improve automatically with experience
- Imitating human learning
  - Human learning
    - Fast recognition and classification of complex classes of objects and concepts and fast adaptation
  - Example: neural networks
- Some techniques assume statistical source
  - Select a statistical model to model the source
- Other techniques are based on reasoning or inductive inference (e.G. Decision tree)

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# Disciplines Relevant to ML

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- Artificial intelligence
- Bayesian methods
- Control theory
- Information theory
- Computational complexity theory
- Philosophy
- Psychology and neurobiology
- Statistics

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# Machine Learning Definition

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A computer program is said to **learn** from *experience*  $E$  with respect to some class of *tasks*  $T$  and *performance measure*  $P$ , if its performance at tasks in  $T$ , as measured by  $P$ , improves with experience.

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## Examples of Learning Problems

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### *Example 1: handwriting recognition:*

- T: recognizing and classifying handwritten words within images.
- P: percentage of words correctly classified.
- E: a database of handwritten words with given classification.

### *Example 2: learn to play checkers:*

- T: play checkers.
- P: percentage of games won in a tournament.
- E: opportunity to play against itself (**war games...**).

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## Type of Training Experience

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### ■ **Direct or indirect?**

- Direct: board state -> correct move
- Indirect: credit assignment problem (degree of credit or blame for each move to the final outcome of win or loss)

### ■ **Teacher or not ?**

- Teacher selects board states and provide correct moves **or**
- Learner can select board states

### ■ **Is training experience representative of performance goal?**

- Training playing against itself
- Performance evaluated playing against world champion

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## Issues in *Machine Learning*

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- What algorithms can approximate functions well and when?
- How does the number of training examples influence accuracy?
- How does the complexity of hypothesis representation impact it?
- How does noisy data influence accuracy?
- *How do you reduce a learning problem to a set of function approximation ?*

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## Summary

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- *Machine learning* is useful for data mining, poorly understood domain (face recognition) and programs that must dynamically adapt.
- Draws from many diverse disciplines.
- Learning problem needs well-specified task, performance metric and training experience.
- Involve searching space of possible hypotheses. Different learning methods search different hypothesis space, such as numerical functions, *neural networks*, decision trees, symbolic rules.

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# Topics in Neural Networks

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## Lecture 2: Introduction

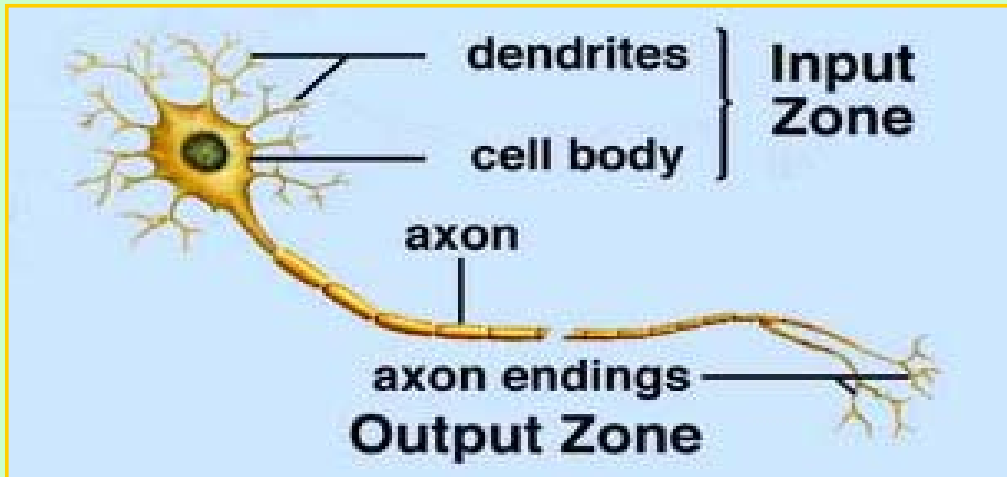


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# Introduction to Neural Networks

# Brain

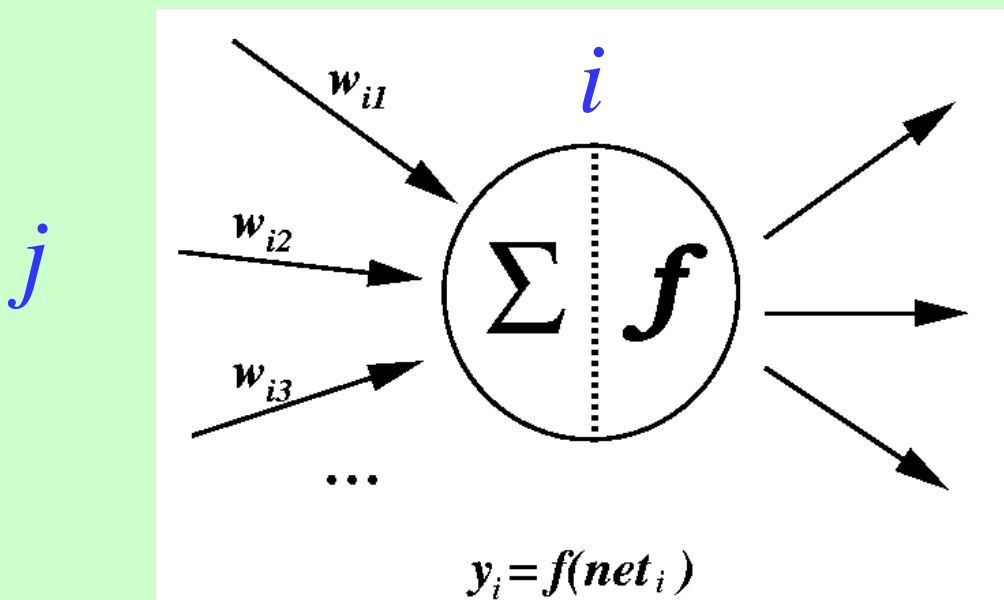
- $10^{11}$  neurons (processors)
- On average 1000-10000 connections



# Artificial Neuron

$$net_i = \sum_j w_{ij}y_j + b$$

bias





# Artificial Neuron

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- Input/Output Signal may be.
  - Real value.
  - Unipolar  $\{0, 1\}$ .
  - Bipolar  $\{-1, +1\}$ .
- Weight :  $w_{ij}$  – strength of connection.

Note that  $w_{ij}$  refers to the weight from **unit  $j$  to unit  $i$**  (not the other way round).



# Artificial Neuron

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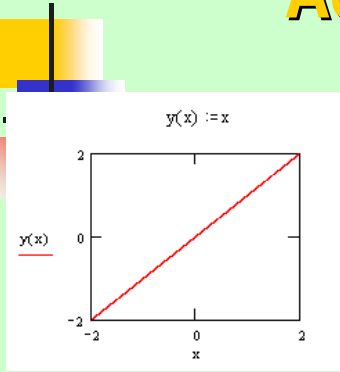
- The bias  $b$  is a constant that can be written as  $w_{i0}y_0$  with  $y_0 = b$  and  $w_{i0} = 1$  such that

$$net_i = \sum_{j=0}^n w_{ij} y_j$$

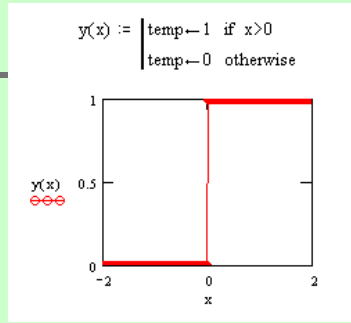
- The function  $f$  is the unit's **activation function**. In the simplest case,  $f$  is the identity function, and the unit's output is just its net input. This is called a **linear unit**.
- Other activation functions are : **step function**, **sigmoid function** and **Gaussian function**.



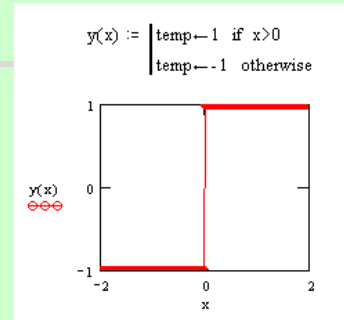
# Activation Functions



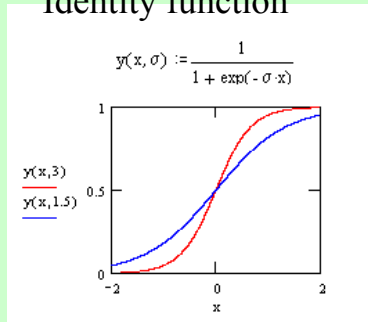
Identity function



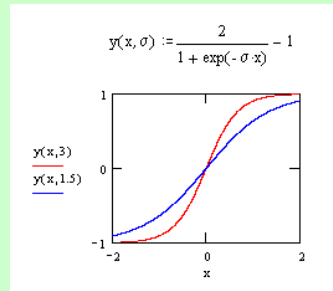
Binary Step function



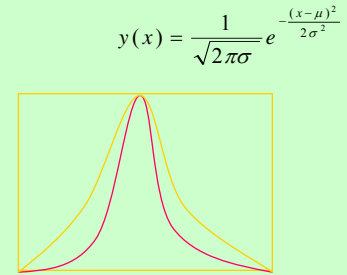
Bipolar Step function



Sigmoid function

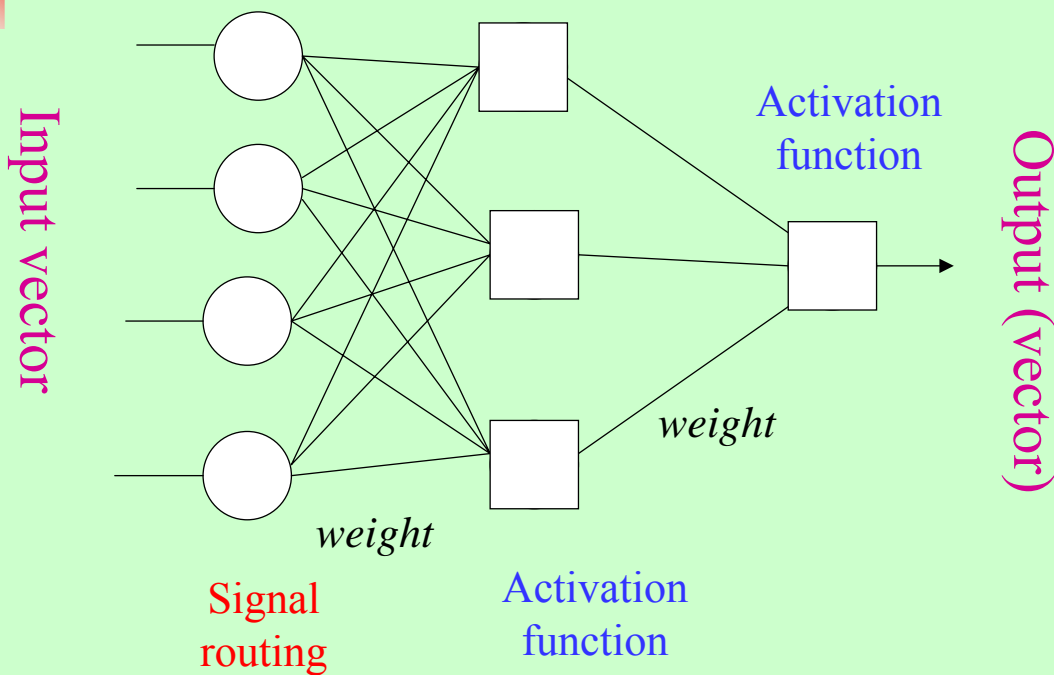


Bipolar Sigmoid function



Gaussian function

# Artificial Neural Networks (ANN)





## Historical Development of ANN...

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- William James (1890) : describes in words and figures simple distributed networks and Hebbian learning
- McCulloch & Pitts (1943) : binary threshold units that perform logical operations (they proof universal computation)
- Hebb (1949) : formulation of a physiological (local) learning rule
- Roseblatt (1958) : the perceptron– a first real learning machine
- Widrow & Hoff (1960) : ADALINE and the Widrow-Hoff supervised learning rule

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## Historical Development of ANN

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- Kohonen (1982) : **Self-organizing maps**
- Hopfield (1982): **Hopfield Networks**
- Rumelhart, Hinton & Williams (1986) : **Back-propagation & Multilayer Perceptron**
- Broomhead & Lowe (1988) : **Radial basis functions (RBF)**
- Vapnik (1990) -- **support vector machine**

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## When Should ANN Solution Be Considered ?

- The solution to the problem cannot be explicitly described by an algorithm, a set of equations, or a set of rules.
- There is some evidence that an input-output mapping exists between a set of input and output variables.
- There should be a large amount of data available to train the network.

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## Problems That Can Lead to Poor Performance ?

- The network has to distinguish between very similar cases with a very high degree of accuracy.
- The train data does not represent the ranges of cases that the network will encounter in practice.
- The network has a several hundred inputs.
- The main discriminating factors are not present in the available data. *E.g.* Trying to assess the loan application without having knowledge of the applicant's salaries.
- The network is required to implement a very complex function.

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## Applications of Artificial Neural Networks

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- Manufacturing : fault diagnosis, fraud detection.
- Retailing : fraud detection, forecasting, data mining.
- Finance : fraud detection, forecasting, data mining.
- Engineering : fault diagnosis, signal/image processing.
- Production : fault diagnosis, forecasting.
- Sales & marketing : forecasting, data mining.

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## Data Pre-processing

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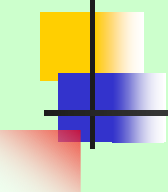
Neural networks very **rarely** operate on the raw data. An initial **pre-processing** stage is essential.

Some examples are as follows:

- Feature extraction of images: for example, the analysis of x-rays requires pre-processing to extract features which may be of interest within a specified region.
- Representing input variables with numbers. For example "+1" is the person is married, "0" if divorced, and "-1" if single. Another example is representing the pixels of an image: 255 = bright white, 0 = black. To ensure the generalization capability of a neural network, the data should be encoded in form which allows for interpolation.

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# Data Pre-processing

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## ■ Categorical Variable

- A categorical variable is a variable that can belong to one of a number of discrete categories. For example, red, green, blue.
- Categorical variables are usually encoded using 1 out-of-n coding. e.g. for three colors, red = (1 0 0), green = (0 1 0) Blue = (0 0 1).
- If we used red = 1, green = 2, blue = 3, then this type of encoding imposes an ordering on the values of the variables which does not exist.

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# Data Pre-processing

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## ■ CONTINUOUS VARIABLES

- A continuous variable can be directly applied to a neural network. However, if the dynamic range of input variables are not approximately the same, it is better to *normalize* all input variables of the neural network.

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## Example of Normalized Input Vector

- Input vector :  $(2\ 4\ 5\ 6\ 10\ 4)^t$
- Mean of vector :  $\mu = \frac{1}{6} \sum_{i=1}^6 x_i = 5.167$
- Standard deviation :  $\sigma = \sqrt{\frac{1}{6-1} \sum_{i=1}^6 (x_i - \mu)^2} = 2.714$
- Normalized vector :  $x_N = \frac{x_i - \mu}{\sigma} = (-1.17\ -0.43\ -0.06\ 0.31\ 1.78\ -0.43)^t$
- Mean of normalized vector is zero
- Standard deviation of normalized vector is unity

## Simple Neural Networks

### Lecture 3: Simple Perceptron

# Outlines

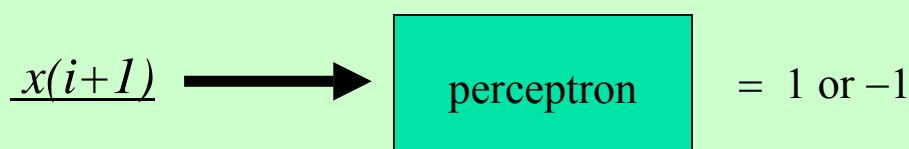
- The Perceptron
  - Linearly separable problem
  - Network structure
  - Perceptron learning rule
  - Convergence of Perceptron

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## THE PERCEPTRON

- The perceptron was a simple model of ANN introduced by Rosenblatt of MIT in the 1960' with the idea of learning.
- Perceptron is designed to accomplish a **simple pattern recognition** task: after learning with real value training data  $\{ \underline{x(i)}, d(i), i = 1, 2, \dots, p \}$  where  $d(i) = 1$  or  $-1$
- For a new signal (pattern)  $\underline{x(i+1)}$ , the perceptron is capable of telling you to which class the new signal belongs

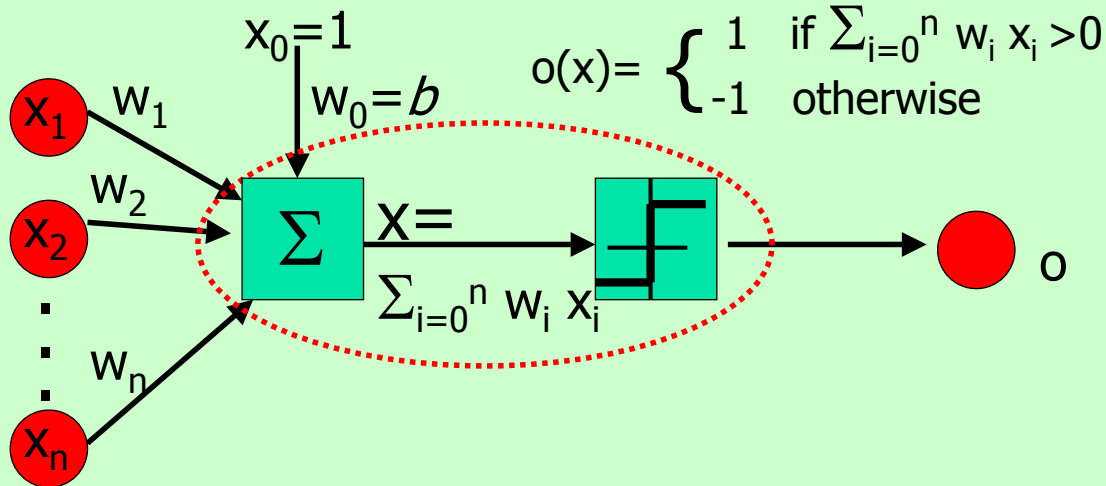


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# Perceptron

## Linear Threshold Unit (LTU)



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## Mathematically the Perceptron is

$$y = f\left(\sum_{i=1}^m w_i x_i + b\right) = f\left(\sum_{i=0}^m w_i x_i\right)$$

We can always treat the bias  $b$  as another weight with inputs equal 1

where  $f$  is the hard limiter function i.e.

$$y = \begin{cases} 1 & \text{if } \sum_{i=1}^m w_i x_i + b > 0 \\ -1 & \text{if } \sum_{i=1}^m w_i x_i + b \leq 0 \end{cases}$$

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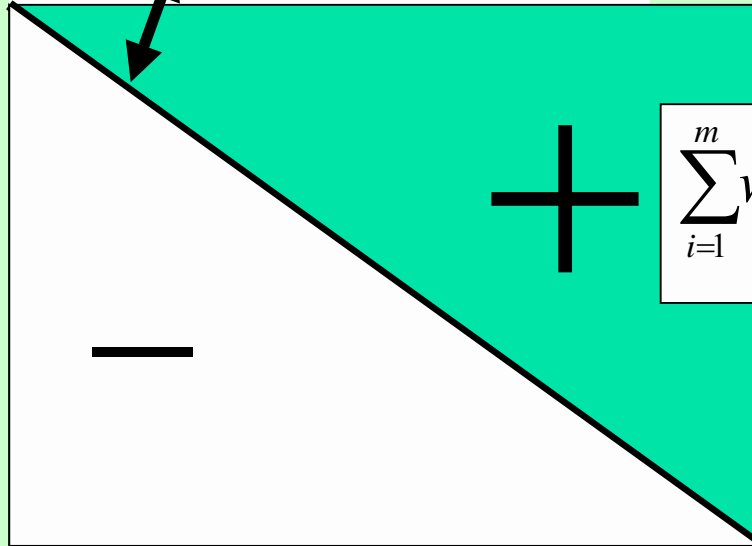


## Why is the network capable of solving linearly separable problem ?

$$\sum_{i=1}^m w_i x_i + b = 0$$

$$\sum_{i=1}^m w_i x_i + b < 0$$

$$\sum_{i=1}^m w_i x_i + b > 0$$



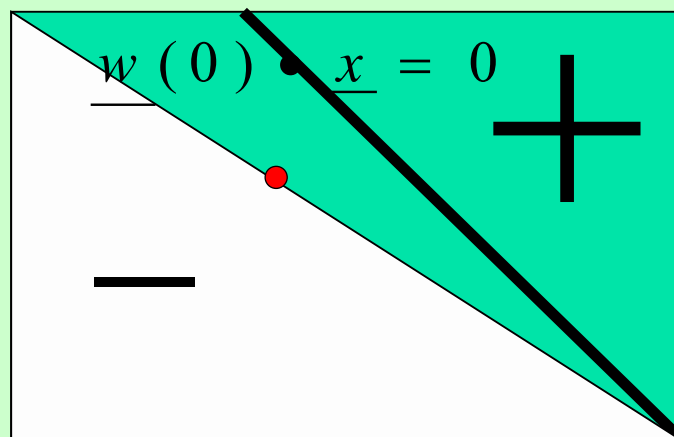
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## Learning rule

An algorithm to update the weights  $\underline{w}$  so that finally the input patterns lie on both sides of the line decided by the perceptron

Let  $t$  be the time, at  $t = 0$ , we have

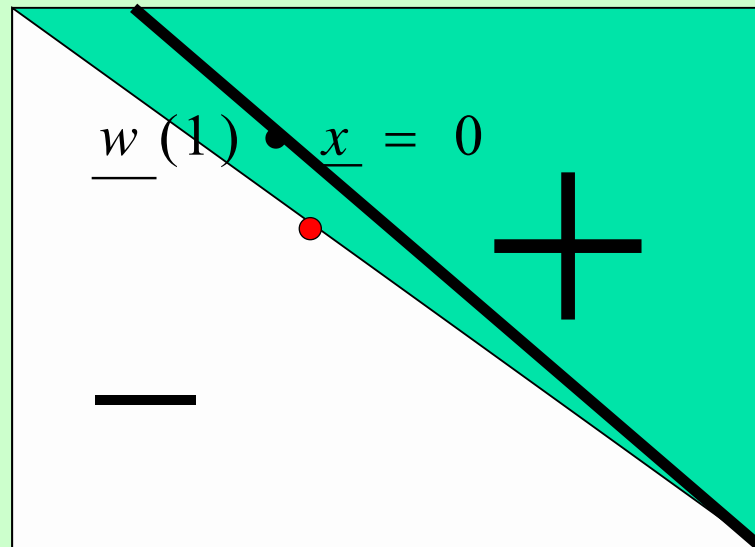


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An algorithm to update the weights  $\underline{w}$  so that finally the input patterns lie on both sides of the line decided by the perceptron

Let  $t$  be the time, at  $t = 1$

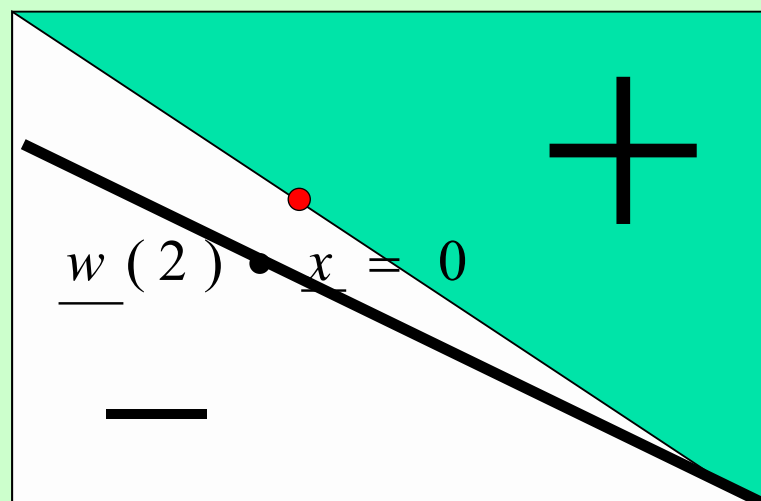


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An algorithm to update the weights  $\underline{w}$  so that finally the input patterns lie on both sides of the line decided by the perceptron

Let  $t$  be the time, at  $t = 2$



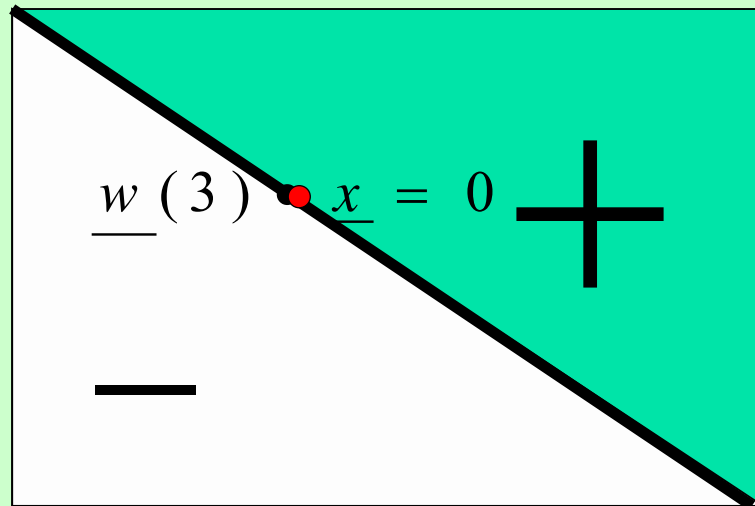
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## Learning rule

An algorithm to update the weights  $\underline{w}$  so that finally the input patterns lie on both sides of the line decided by the perceptron

Let  $t$  be the time, at  $t = 3$



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## In Math

$$d(t) = \begin{cases} +1 & \text{if } x(t) \text{ in class } + \\ -1 & \text{if } x(t) \text{ in class } - \end{cases}$$

### Perceptron learning rule

$$\underline{w}(t+1) = \underline{w}(t) + \eta(t) [d(t) - \text{sign}(\underline{w}(t) \cdot \underline{x}(t))] \underline{x}(t)$$

Where  $\eta(t)$  is the learning rate  $>0$ ,

$$\text{sign}(x) = \begin{cases} +1 & \text{if } x > 0 \\ -1 & \text{if } x \leq 0, \end{cases} \quad \text{hard limiter function}$$

NB :  $d(t)$  is the same as  $d(i)$  and  $x(t)$  as  $x(i)$

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## In words:

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- If the classification is right, do not update the weights
- If the classification is not correct, update the weight towards the opposite direction so that the output move close to the right directions.



## Perceptron convergence theorem (Rosenblatt, 1962)

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Let the subsets of training vectors be linearly separable. Then after finite steps of learning we have

**$\lim \underline{w}(t) = \underline{w}$  which correctly separate the samples.**

The idea of proof is that to consider  $||\underline{w}(t+1) - \underline{w}|| - ||\underline{w}(t) - \underline{w}||$  which is a decrease function of  $t$

# Summary of Perceptron learning ...

## Variables and parameters

$$\underline{x}(t) = (m+1) \text{ dim. input vectors at time } t \\ = ( b, x_1(t), x_2(t), \dots, x_m(t) )$$

$$\underline{w}(t) = (m+1) \text{ dim. weight vectors} \\ = ( 1, w_1(t), \dots, w_m(t) )$$

$b$  = bias

$y(t)$  = actual response

$\eta(t)$  = learning rate parameter, a +ve constant  $< 1$

$d(t)$  = desired response

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# Summary of Perceptron learning ...

~~Data~~  $\{ (\underline{x}(i), d(i)), i=1, \dots, p \}$

✓ Present the data to the network once a point

✓ could be cyclic :

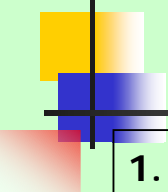
$$(\underline{x}(1), d(1)), (\underline{x}(2), d(2)), \dots, (\underline{x}(p), d(p)), \\ (\underline{x}(p+1), d(p+1)), \dots$$

✓ or randomly

*(Hence we mix time  $t$  with  $i$  here)*

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## Summary of Perceptron learning (algorithm)

1. **Initialisation** Set  $\underline{w}(0)=0$ . Then perform the following computation for time step  $t=1,2,\dots$
2. **Activation** At time step  $t$ , activate the perceptron by applying input vector  $\underline{x}(t)$  and desired response  $d(t)$
3. **Computation of actual response** Compute the actual response of the perceptron

$$y(t) = \text{sign} ( \underline{w}(t) \cdot \underline{x}(t) )$$

where *sign* is the sign function

4. **Adaptation of weight vector** Update the weight vector of the perceptron

$$\underline{w}(t+1) = \underline{w}(t) + \eta(t) [ d(t) - y(t) ] \underline{x}(t)$$

5. **Continuation**



## Questions remain

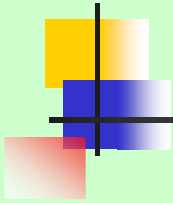
### Where or when to stop?

By minimizing the generalization error

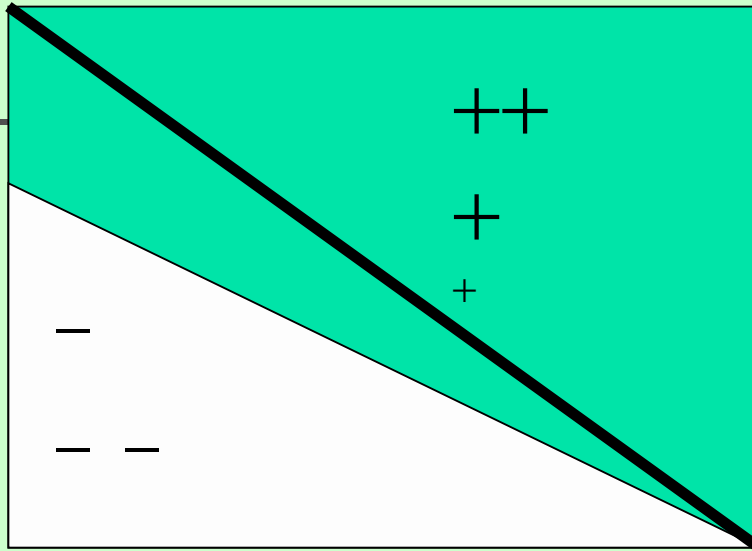
For training data  $\{(\underline{x}(i), d(i)), i=1,\dots,p\}$

How to define training error after  $t$  steps of learning?

$$E(t) = \sum_{i=1}^p [d(i) - \text{sign}(\underline{w}(t) \cdot \underline{x}(i))]^2$$



After learning t steps



$$E(t) = 0$$

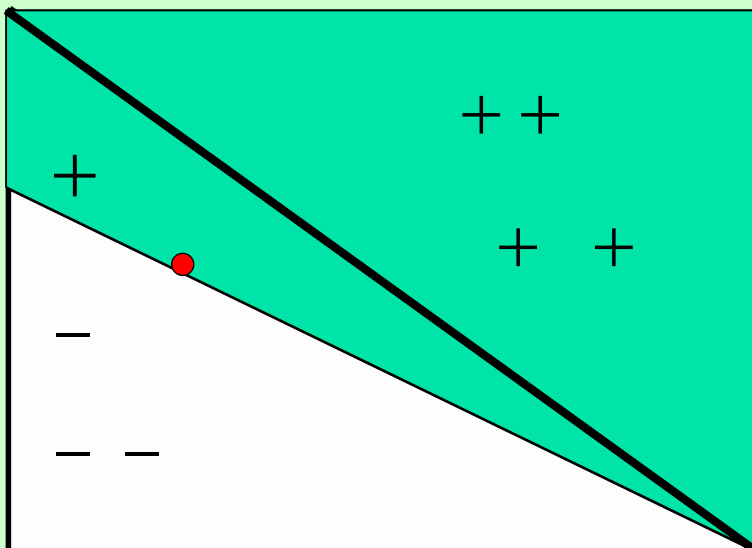
## How to define generalisation error?

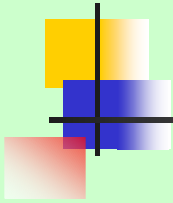


For a new signal  $\{\underline{x}(t+1), d(t+1)\}$ , we have

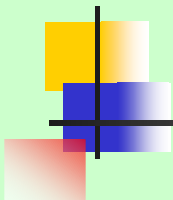
$$E_g = [d(t+1) - \text{sign}(\underline{x}(t+1) \bullet \underline{w}(t))]^2$$

After learning t steps





We next turn to **ADALINE learning**,  
from which we can understand  
the learning rule, and more general the  
**Back-Propagation (BP) learning**



# Simple Neural Network

## Lecture 4: ADALINE Learning



# Outlines

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- ADALINE
- Gradient descending learning
- Modes of training

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# Unhappy Over Perceptron Training

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- When a perceptron gives the right answer, no learning takes place
- Anything below the threshold is interpreted as **'no', even it is just below the threshold.**
- It might be better to train the neuron based on **how far below the threshold it is.**

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# ADALINE

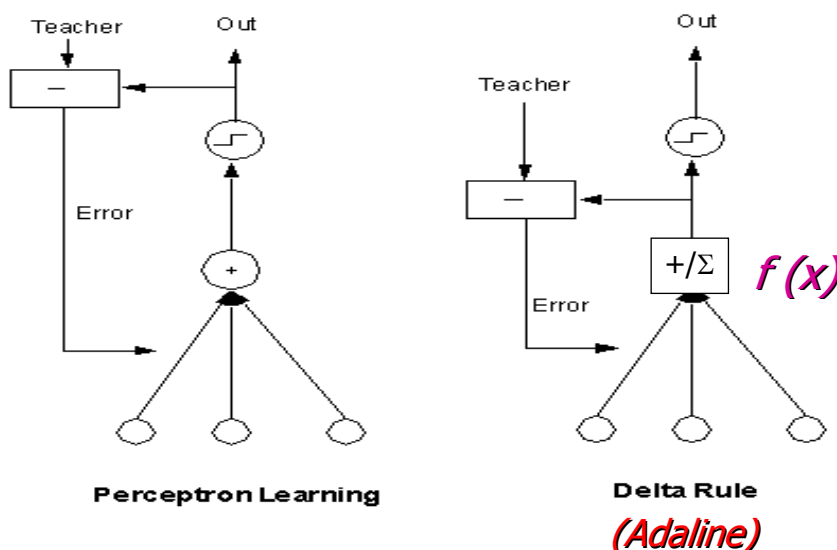
- **ADALINE** is an acronym for ADAPtive LINear Element (or ADAPtive LINear NEuron) developed by Bernard Widrow and Marcian Hoff (1960).
- There are several variations of Adaline. One has threshold same as perceptron and another just a bare linear function.
- The **Adaline learning** rule is also known as the least-mean-squares (LMS) rule, the delta rule, or the Widrow-Hoff rule.
- It is a training rule that minimizes the output error using (approximate) gradient descent method.

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- Replace the step function in the perceptron with a **continuous (differentiable) function  $f$** , e.g the simplest is **linear function**

- With or without the threshold, the **Adaline** is trained based on the output of the function  $f$  rather than the final output.



After each training pattern  $\underline{x}(i)$  is presented, **the correction to apply to the weights is proportional to the error.**

$$E(i,t) = \frac{1}{2} [d(i) - f(\underline{w}(t) \cdot \underline{x}(i))]^2 \quad i=1,\dots,p$$

*N.B.* If  $f$  is a **linear function**  $f(\underline{w}(t) \cdot \underline{x}(i)) = \underline{w}(t) \cdot \underline{x}(i)$

Summing together, our purpose is to find  $\underline{W}$  which minimizes

$$E(t) = \sum_j E(i,t)$$

## General Approach gradient descent method

To find  $g$

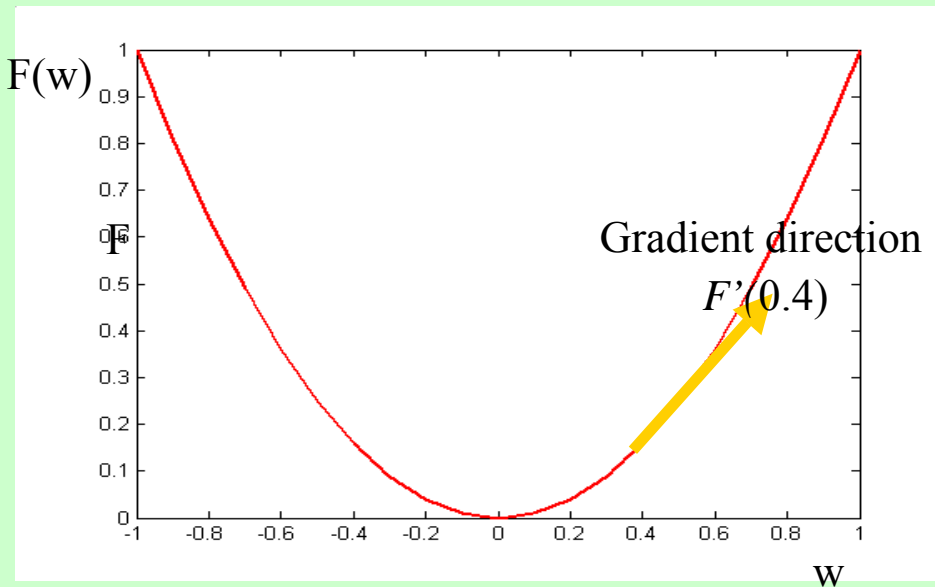
$$\underline{w}(t+1) = \underline{w}(t) + g(E(\underline{w}(t)))$$

so that  $\underline{w}$  automatically tends to the global minimum of  $E(w)$ .

$$\underline{w}(t+1) = \underline{w}(t) - E'(\underline{w}(t))\eta(t)$$

*(see figure below)*

- Gradient direction is the direction of uphill  
for example, in the Figure, at position 0.4, the  
gradient is uphill ( F is E, consider one dim case )



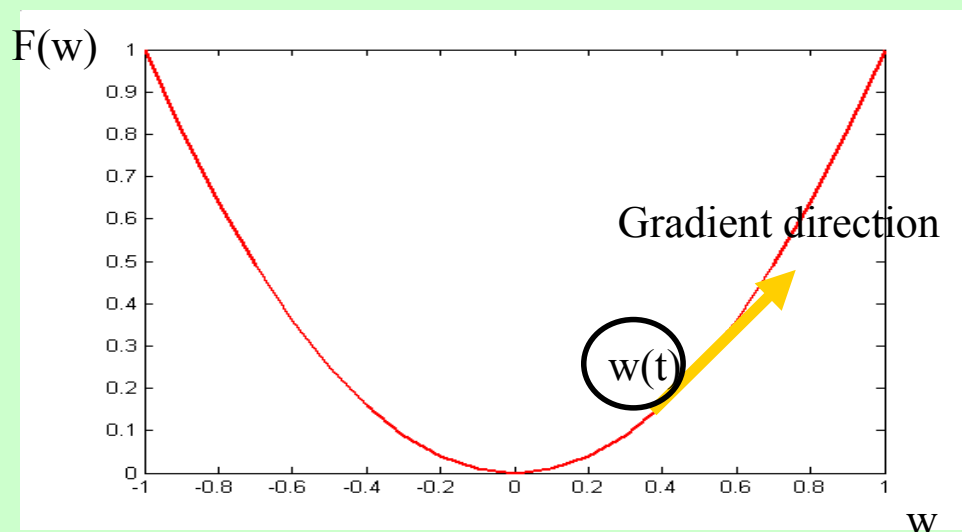
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- In gradient descent algorithm, we have

$$\underline{w}(t+1) = \underline{w}(t) - F'(w(t)) \eta(\tau)$$

therefore the ball goes downhill since  $-F'(w(t))$   
is downhill direction



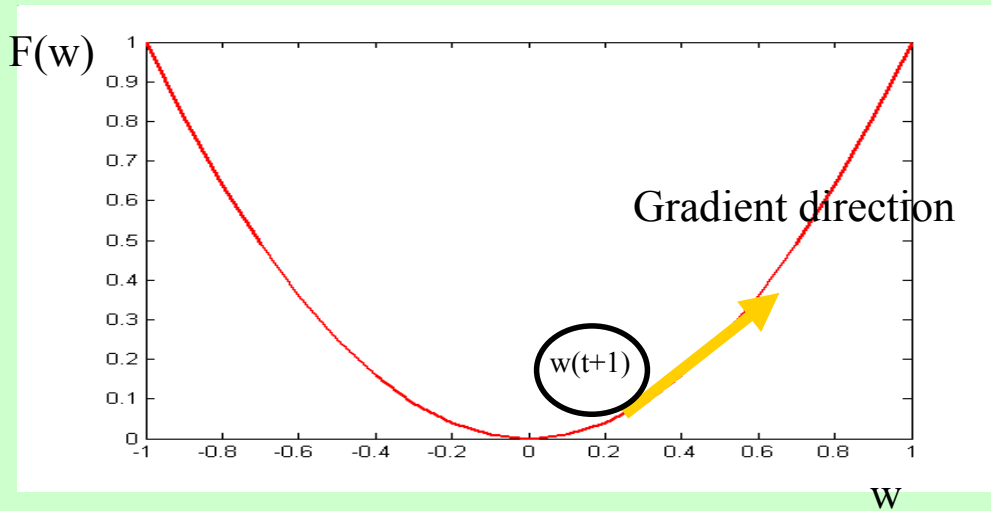
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- In gradient descent algorithm, we have

$$w(t+1) = w(t) - F'(w(t)) \eta(\tau)$$

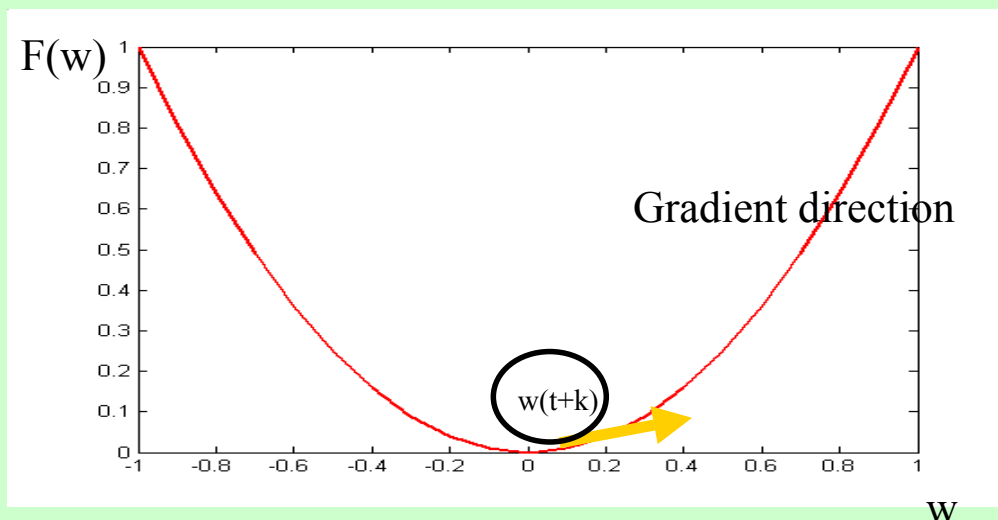
therefore the ball goes downhill since  $-F'(w(t))$  is downhill direction



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- Gradually the ball will stop at a **local minima** where the gradient is zero



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## • In words

**Gradient method could be thought of as a ball rolling down from a hill: the ball will roll down and finally stop at the valley**

Thus, the weights are adjusted by

$$w_j(t+1) = w_j(t) + \eta(t) \sum [d(i) - f(\underline{w}(t) \cdot \underline{x}(i))] x_j(i) f'$$

This corresponds to gradient descent on the quadratic error surface E

When  $f' = 1$ , we have the perceptron learning rule (we have in general  $f' > 0$  in neural networks). The ball moves in the right direction.



## Two types of network training:

**Sequential mode** (on-line, stochastic, or per-pattern) :

*Weights updated after each pattern is presented (Perceptron is in this class)*

**Batch mode** (off-line or per-epoch) :

*Weights updated after all patterns are presented*

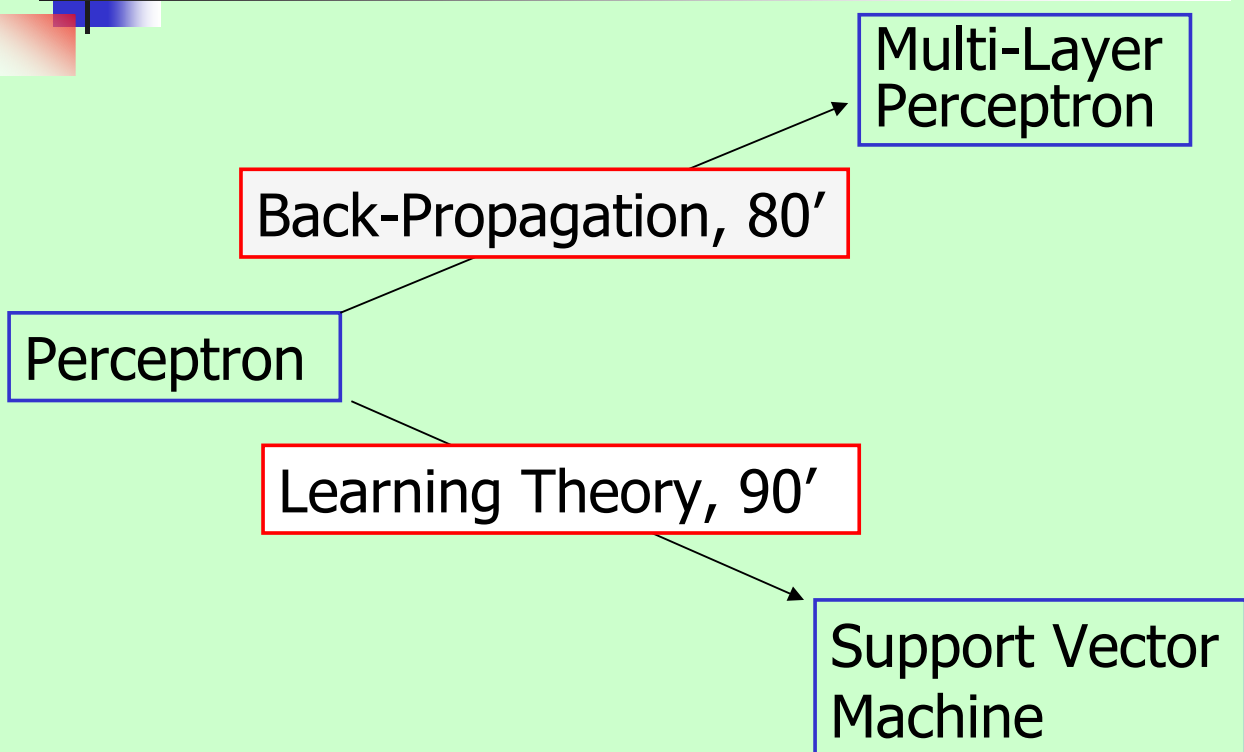
# Comparison Perceptron and Gradient Descent Rules

- **Perceptron learning rule** guaranteed to succeed if
  - Training examples are **linearly separable**
  - Sufficiently small learning rate  $\eta$
- **Linear unit training rule** uses gradient descent guaranteed to converge to hypothesis with minimum squared error given sufficiently small learning rate  $\eta$ 
  - Even when training data contains noise
  - Even when training data **not separable by hyperplanes**

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# Renaissance of Perceptron



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# Summary

---

## Perceptron

$$\underline{W}(t+1) = \underline{W}(t) + \eta(t) [d(t) - \text{sign}(\underline{w}(t) \cdot \underline{x})] \underline{x}$$

## Adaline (Gradient descent method)

$$\underline{W}(t+1) = \underline{W}(t) + \eta(t) [d(t) - f(\underline{w}(t) \cdot \underline{x})] \underline{x} f'$$



# Multi-Layer Perceptron (MLP)

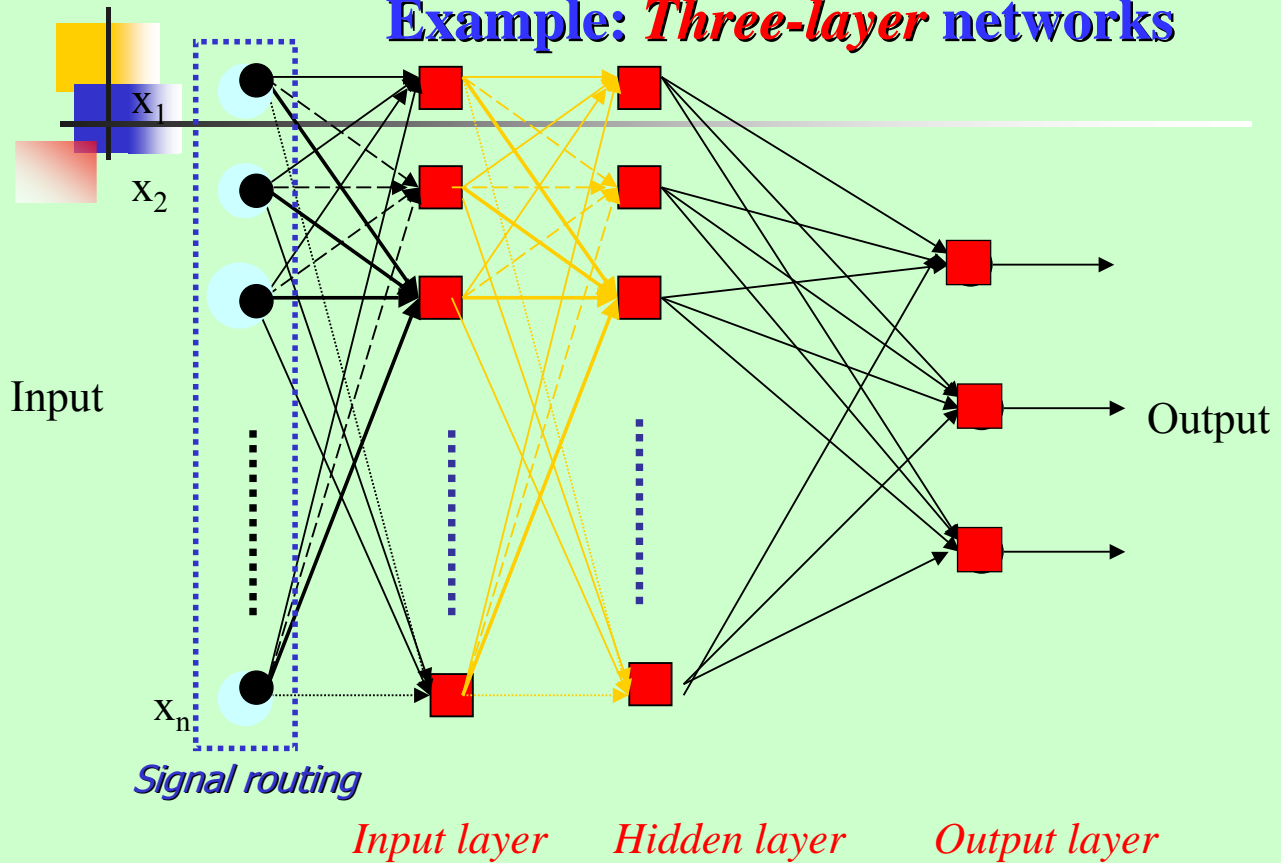
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## *Idea: Credit assignment problem*

- Problem of assigning 'credit' or 'blame' to individual elements involving in forming overall response of a learning system (hidden units)
- In **neural networks**, problem relates to dividing which weights should be altered, **by how much and in which direction**.



## Example: *Three-layer* networks

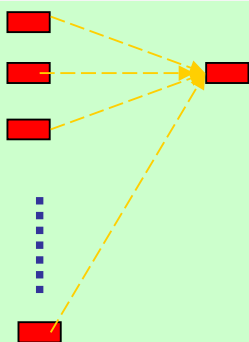


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## Properties of architecture

- No connections within a layer
- No direct connections between input and output layers
- Fully connected between layers
- Often more than 2 layers
- Number of output units need not equal number of input units
- Number of hidden units per layer can be more or less than input or output units



Each unit '■' is a perceptron

$$y_i = f \left( \sum_{j=1}^m w_{ij} x_j + b_i \right)$$

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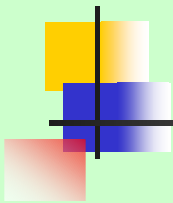
# BP (Back Propagation)

---

gradient descent method

+

multilayer networks



## Lecture 5

# MultiLayer Perceptron I

---

## Back Propagating Learning

# BP learning algorithm

## Solution to "credit assignment problem" in MLP

Rumelhart, Hinton and Williams (1986)

BP has two phases:

**Forward pass phase:** computes 'functional signal', feedforward propagation of input pattern signals through network

**Backward pass phase:** computes 'error signal', propagation of error (difference between actual and desired output values) backwards through network starting at output units

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# BP Learning for Simplest MLP<sub>O</sub>

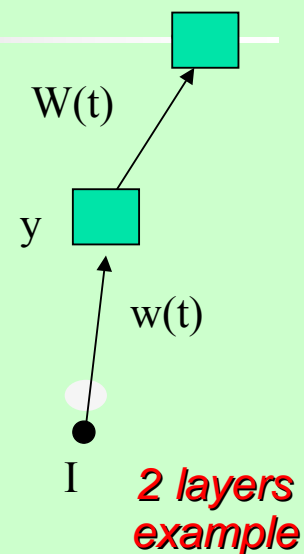
Task : Data  $\{I, d\}$  to minimize

$$\begin{aligned} E &= (d - o)^2 / 2 \\ &= [d - f(W(t)y(t))]^2 / 2 \\ &= [d - f(W(t)f(w(t)I))]^2 / 2 \end{aligned}$$

Error function at the output unit

Weight at time  $t$  is  $w(t)$  and  $W(t)$ , intend to find the weight  $w$  and  $W$  at time  $t+1$

Where  $y = f(w(t)I)$ , output of the **input unit**



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# Forward pass phase

Suppose that we have  $w(t)$ ,  $W(t)$  of time  $t$

For given input  $I$ , we can calculate

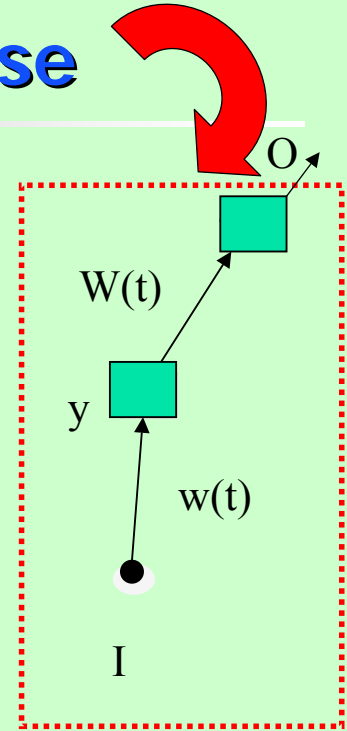
$$y = f(w(t)I)$$

and

$$o = f(W(t)y) = f(W(t)f(w(t)I))$$

Error function of output unit will be

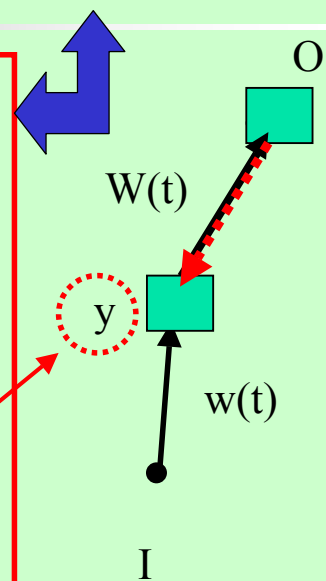
$$E = (d - o)^2 / 2$$



2 layers example

# Backward Pass Phase

$$\begin{aligned} W(t+1) &= W(t) - \eta \frac{dE}{dW(t)} \\ &= W(t) - \eta \frac{dE}{df} \frac{df}{dW(t)} \\ &= W(t) + \eta (d - o) f'(W(t)y) y \end{aligned}$$

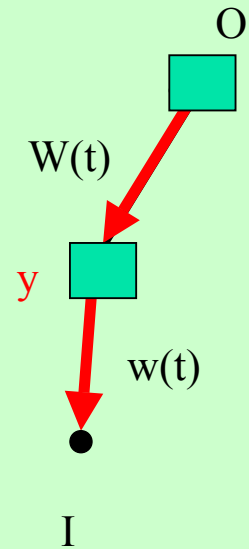


$$E = (d - o)^2 / 2$$

$$o = f(W(t)y)$$

# Backward pass phase

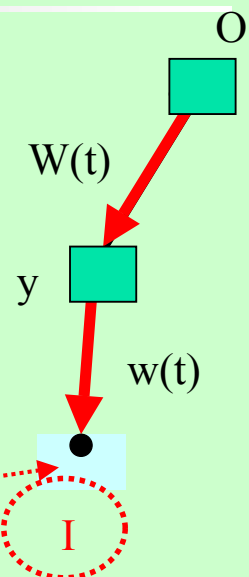
$$\begin{aligned}
 W(t+1) &= W(t) - \eta \frac{dE}{dW(t)} \\
 &= W(t) - \eta \frac{dE}{df} \frac{df}{dW(t)} \\
 &= W(t) + \eta(d - o) f'(W(t)y) y \\
 &= W(t) + \eta \Delta y
 \end{aligned}$$



where  $\Delta = (d - o) f'$

# Backward pass phase

$$\begin{aligned}
 w(t+1) &= w(t) - \eta \frac{dE}{dw(t)} \\
 &= w(t) - \eta \frac{dE}{dy} \frac{dy}{dw(t)} \\
 &= w(t) + \eta(d - o) f'(W(t)y) W(t) \frac{dy}{dw(t)} \\
 &= w(t) + \eta \Delta W(t) f'(w(t)I) I
 \end{aligned}$$



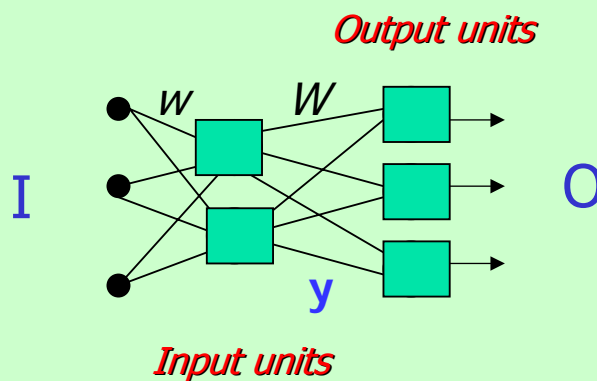
$$\begin{aligned}
 o &= f(W(t)y) \\
 &= f(W(t) f(w(t)I))
 \end{aligned}$$

# Review:

## General Two Layer Network

$I$  inputs,  $O$  outputs,  $w$  connections for input units,  $W$  connections for output units,  $y$  is the activity of input unit

$net(t)$  = network input to the unit at time  $t$



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## Forward pass

Weights are fixed during forward & backward pass

### 1. Compute values for input units

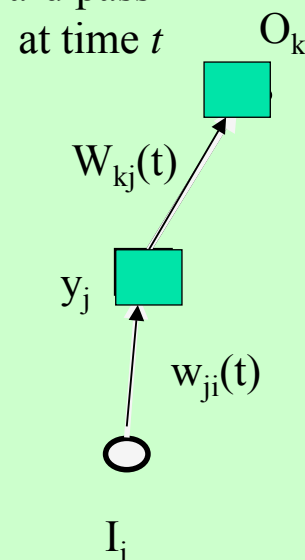
$$net_j(t) = \sum_i w_{ji}(t) I_i(t)$$

$$y_j = f(net_j(t))$$

### 2. compute values for output units

$$Net_k(t) = \sum_j W_{kj}(t) y_j$$

$$O_k = f(Net_k(t))$$



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Recall delta rule , error measure for pattern n is

$$E(t) = \frac{1}{2} \sum_{k=1} (d_k(t) - O_k(t))^2$$

We want to know **how to modify weights in order to decrease E** where

$$w_{ij}(t+1) - w_{ij}(t) \propto - \frac{\partial E(t)}{\partial w_{ij}(t)}$$

**both for input units and output units**

This can be rewritten as product of two terms using chain rule

$$\frac{\partial E(t)}{\partial w_{ij}(t)} = \frac{\partial E(t)}{\partial net_j(t)} \cdot \frac{\partial net_j(t)}{\partial w_{ij}(t)}$$

**both for input units and output units**

Term A

How error for pattern changes as function of change in network input to unit  $j$

Term B

How net input to unit  $j$  changes as a function of change in weight  $w$

**weight updates are local**

$$w_{ji}(t+1) - w_{ji}(t) = \eta \delta_j(t) I_i(t) \quad (\text{input unit})$$

$$W_{kj}(t+1) - W_{kj}(t) = \eta \Delta_k(t) y_j(t) \quad (\text{output unit})$$

**output unit**

$$\begin{aligned} W_{kj}(t+1) - W_{kj}(t) &= \eta \Delta_k(t) y_j(t) \\ &= \eta (d_k(t) - O_k(t)) f'(Net_k(t)) y_j(t) \end{aligned}$$

**input unit**

$$\begin{aligned} w_{ji}(t+1) - w_{ji}(t) &= \eta \delta_j(t) I_i(t) \\ &= \eta f'(net_j(t)) \sum_k \Delta_k(t) W_{kj} I_i(t) \end{aligned}$$

Once weight changes are computed for all units, weights are updated at same time (bias included as weights here)

We now compute the **derivative of the activation function**  $f(\cdot)$ .

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**Activation Functions**

➤ to compute  $\delta_j$  and  $\Delta_k$  we need to find the derivative of activation function  $f$

➤ to find derivative the activation function must be smooth

Sigmoidal (logistic) function-common in MLP

$$f(net_i(t)) = \frac{1}{1 + \exp(-knet_i(t))}$$

where  $k$  is a positive constant. The sigmoidal function gives value in range of 0 to 1

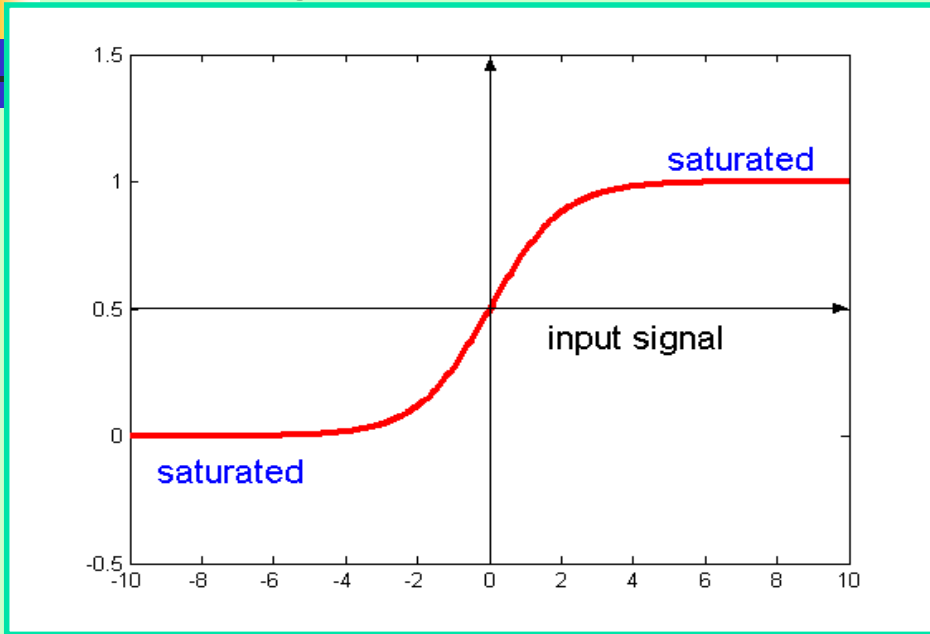
*Input-output function of a neuron (rate coding assumption)*

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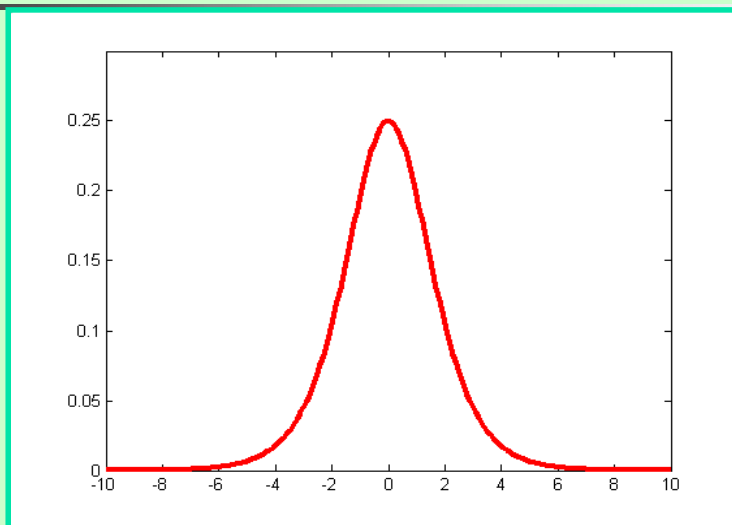


# Shape of sigmoidal function



Note: when net = 0, f = 0.5

# Shape of sigmoidal function derivative



Derivative of sigmoidal function has max at  $x=0$ , is symmetric about this point falling to zero as sigmoidal approaches extreme values

Returning to **local error gradients** in BP algorithm we have for **output units**

$$\begin{aligned}\Delta_i(t) &= (d_i(t) - O_i(t)) f'(Net_i(t)) \\ &= (d_i(t) - O_i(t)) kO_i(t)(1 - O_i(t))\end{aligned}$$

For **input units** we have

$$\begin{aligned}\delta_i(t) &= f'(net_i(t)) \sum_k \Delta_k(t) W_{ki} \\ &= ky_i(t)(1 - y_i(t)) \sum_k \Delta_k(t) W_{ki}\end{aligned}$$

Since degree of weight change is **proportional to derivative of activation function**, weight changes will be greatest when units receives mid-range functional signal than at extremes

## Summary of BP learning algorithm

Set learning rate  $\eta$

Set initial weight values (incl.. biases):  $w, W$

Loop until stopping criteria satisfied:

*present input pattern to NN inputs  
compute functional signal for input units  
compute functional signal for output units*

*present Target response to output units  
compute error signal for output units  
compute error signal for input units  
update all weights at same time  
increment  $n$  to  $n+1$  and select next  $I$  and  $d$*

*end loop*

## Network training:

- ❖ Training set shown repeatedly until stopping criteria are met
- ❖ Each full presentation of all patterns = 'epoch'
- ❖ Randomise order of training patterns presented for each epoch in order to avoid correlation between consecutive training pairs being learnt (order effects)

### Two types of network training:

- **Sequential mode** (on-line, stochastic, or per-pattern)  
Weights updated after each pattern is presented
- **Batch mode** (off-line or per -epoch)

## Advantages and disadvantages of different modes

### Sequential mode:

- Less storage for each weighted connection
- Random order of presentation and updating per pattern means search of weight space is stochastic-reducing risk of local minima able to take advantage of any redundancy in training set (*i.e.* same pattern occurs more than once in training set, esp. for large training sets)
- Simpler to implement

### Batch mode:

- Faster learning than sequential mode

# Lecture 5

## MultiLayer Perceptron II

### Dynamics of MultiLayer Perceptron

Lecture Notes by Prof. Dr. A. A. S. Simani

## Summary of Network Training

Dr. A. A. S. Simani

**Forward phase:**  $\underline{I}(t), \underline{w}(t), \underline{net}(t), \underline{y}(t), \underline{W}(t), \underline{Net}(t), \underline{O}(t)$

**Backward phase:**

**Output unit**

$$W_{kj}(t+1) - W_{kj}(t) = \eta \Delta_k(t) y_j(t)$$

$$= \eta (d_k(t) - O_k(t)) f'(Net_k(t)) y_j(t)$$

**Input unit**

$$w_{ji}(t+1) - w_{ij}(t) = \eta \delta_j(t) I_i(t)$$

$$= \eta f'(net_j(t)) \sum_k \Delta_k(t) W_{kj}(t) I_i(t)$$



## Network training:

---

Training set shown repeatedly until stopping criteria are met.

### Possible convergence criteria are

- Euclidean norm of the gradient vector reaches a sufficiently small denoted as  $\theta$ .
- When the absolute rate of change in the average squared error per epoch is sufficiently small denoted as  $\theta$ .
- **Validation** for generalization performance : stop when generalization reaching the peak (illustrate in this lecture)



## Network training:

---

### Two types of network training:

- **Sequential mode** (on-line, stochastic, or per-pattern)  
Weights updated after each pattern is presented
- **Batch mode** (off-line or per -epoch)  
Weights updated after all the patterns are presented

## Advantages and disadvantages of different modes

### Sequential mode:

- Less storage for each weighted connection
- Random order of presentation and updating per pattern means search of weight space is stochastic--reducing risk of local minima able to take advantage of any redundancy in training set (i.e.. same pattern occurs more than once in training set, esp. for large training sets)
- Simpler to implement

### Batch mode:

- Faster learning than sequential mode

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## Goals of Neural Network Training

To give the correct output for input training vector (**Learning**)

To give good responses to new unseen input patterns (**Generalization**)

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## Training and Testing Problems

- **Stuck neurons:** Degree of weight change is proportional to derivative of activation function, weight changes will be greatest when units receives mid-range functional signal than at extremes neuron. To avoid stuck neurons weights initialization should give outputs of all neurons approximate 0.5
- **Insufficient number of training patterns:** In this case, the training patterns will be learnt instead of the underlying relationship between inputs and output, i.e. network just memorizing the patterns.
- **Too few hidden neurons:** network will not produce a good model of the problem.
- **Over-fitting:** the training patterns will be learnt instead of the underlying function between inputs and output because of too many of hidden neurons. This means that the network will have a poor generalization capability.

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## Dynamics of BP learning

Aim is to minimise an error function over all training patterns by adapting weights in MLP

Recalling the typical error function is the mean squared error as follows

$$E(t) = \frac{1}{2} \sum_{k=1}^p (d_k(t) - O_k(t))^2$$

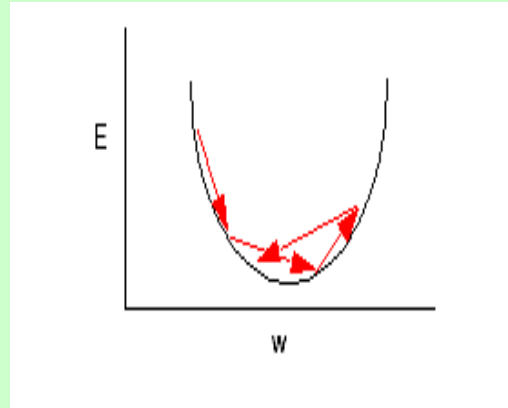
The idea is to reduce  $E(t)$  to global minimum point.

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# Dynamics of BP learning

In **single layer perceptron** with linear activation functions, the error function is simple, described by a smooth parabolic surface with a single minimum

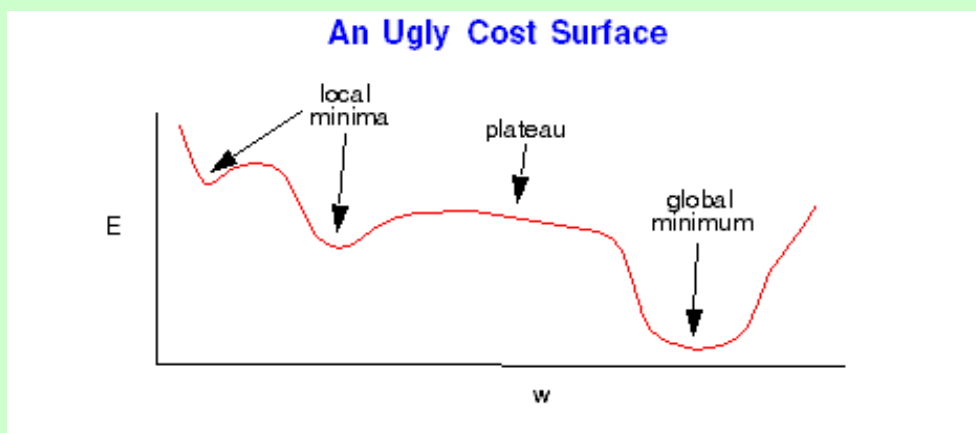


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# Dynamics of BP learning

**MLP with nonlinear activation functions have complex error surfaces** (e.g. plateaus, long valleys etc. ) with no single minimum



For complex error surfaces the problem is learning rate must keep small to prevent divergence. **Adding momentum term is a simple approach dealing with this problem.**

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## Momentum

- Reducing problems of instability while increasing the rate of convergence
- Adding term to weight update equation can effectively holds as exponentially weight history of previous weights changed

Modified weight update equation is

$$w_{ij}(n+1) - w_{ij}(n) = \eta \delta_j(n) y_i(n) + \alpha [w_{ij}(n) - w_{ij}(n-1)]$$

## Effect of momentum term

- If weight changes tend to have same sign momentum term increases and gradient descent **speed up** convergence on shallow gradient
- If weight changes tend to have opposing signs momentum term decreases and gradient descent **slows** to reduce oscillations (stabilizes)
- Can help escape being trapped in local minima



## Selecting Initial Weight Values

---

- Choice of initial weight values is important as this decides starting position in weight space. That is, how far away from global minimum
- Aim is to select weight values which produce midrange function signals
- Select weight values randomly from uniform probability distribution
- Normalise weight values so number of weighted connections per unit produces midrange function signal

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## Convergence of Backprop

**Avoid local minimum with fast convergence:**

- Add momentum
- Stochastic gradient descent
- Train multiple nets with different initial weights

### **Nature of convergence**

- Initialize weights 'near zero' or initial networks near-linear
- Increasingly non-linear functions possible as training progresses

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## Use of Available Data Set for Training

The available data set is normally split into three sets as follows:

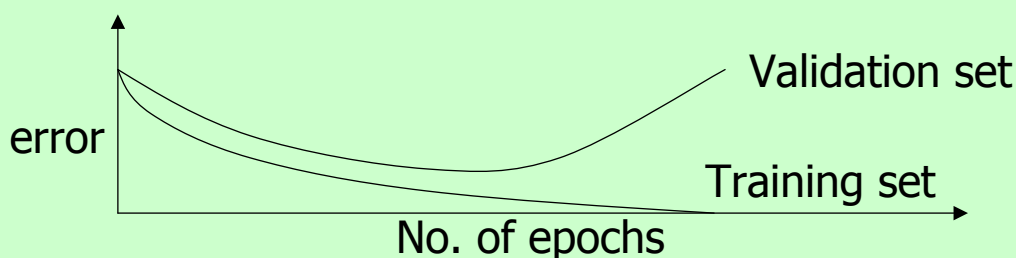
- **Training set** – use to update the weights. Patterns in this set are repeatedly in random order. The weight update equation are applied after a certain number of patterns.
- **Validation set** – use to decide when to stop training only by monitoring the error.
- **Test set** – Use to test the performance of the neural network. It should not be used as part of the neural network development cycle.

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## Earlier Stopping - Good Generalization

- Running too many epochs may **overtrain** the network and result in **overfitting** and perform poorly in generalization.
- Keep a hold-out validation set and test accuracy after every epoch. Maintain weights for best performing network on the validation set and stop training when error increases beyond this.

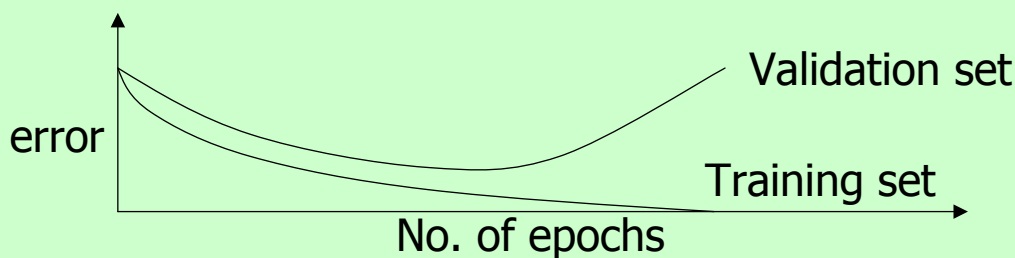


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## Model Selection by Cross-validation

- **Too few hidden units** prevent the network from learning adequately fitting the data and learning the concept (**more than two layer networks**).
- **Too many hidden units** leads to overfitting.
- Similar **cross-validation methods** can be used to determine an appropriate number of hidden units by using the optimal test error to select the model with optimal number of hidden layers and nodes.



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## Alternative training algorithm

### Lecture 8 : Genetic Algorithms

# History Background

- Idea of evolutionary computing was introduced in the 1960s by I. Rechenberg in his work "*Evolution strategies*" (*Evolutionsstrategie* in original). His idea was then developed by other researchers. **Genetic Algorithms** (GAs) were invented by John Holland and developed by him and his students and colleagues. This led to Holland's book "*Adaption in Natural and Artificial Systems*" published in 1975.
- In 1992 John Koza has used **genetic algorithm to evolve programs** to perform certain tasks. He called his method "**Genetic Programming**" (GP). LISP programs were used, because programs in this language can be expressed in the form of a "parse tree", which is the object the GA works

on 17/05/2006

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# Biological Background

## Chromosome.

- All living organisms consist of cells. In each cell there is the same set of **chromosomes**. Chromosomes are strings of **DNA** and serve as a model for the whole organism. **A chromosome consists of genes, blocks of DNA**. Each gene encodes a particular protein. Basically can be said, that each gene encodes a **trait**, for example color of eyes. Possible settings for a trait (e.g. blue, brown) are called **alleles**. Each gene has its own position in the chromosome. This position is called **locus**.
- **Complete set of genetic material (all chromosomes) is called genome**. Particular set of genes in genome is called **genotype**. The genotype is with later development after birth base for the organism's **phenotype**, its physical and mental characteristics, such as eye color, intelligence etc.

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# Biological Background

## Reproduction.

- During reproduction, first occurs **recombination** (or **crossover**). Genes from parents form in some way the whole new chromosome. The new created offspring can then be mutated. **Mutation** means, that the elements of DNA are a bit changed. This changes are mainly caused by errors in copying genes from parents.
- The **fitness** of an organism is measured by **success of the organism in its life**.

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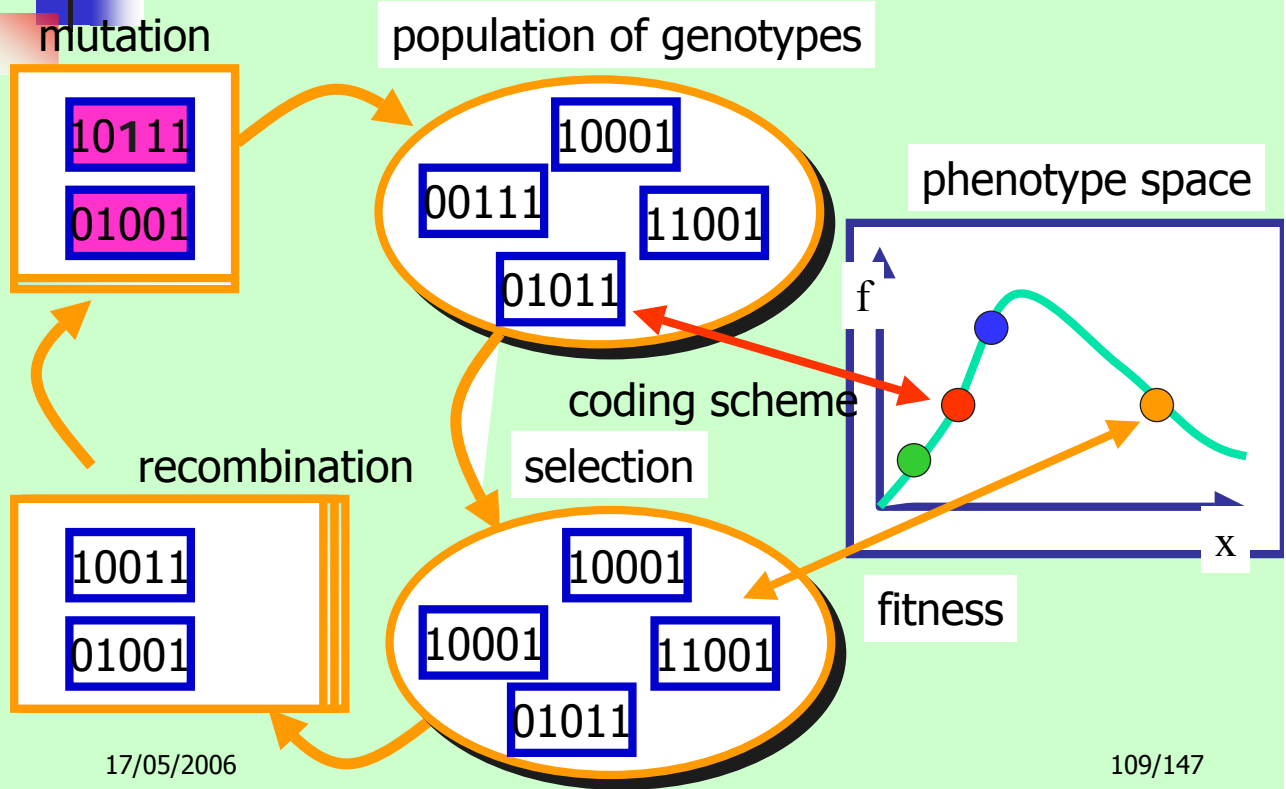
# Evolutionary Computation

- **Based on evolution as it occurs in nature**
  - Lamarck, Darwin, Wallace: evolution of species, survival of the fittest
  - Mendel: genetics provides inheritance mechanism
    - Hence "genetic algorithms"
- **Essentially a massively parallel search procedure**
  - Start with random population of individuals
  - Gradually move to better individuals

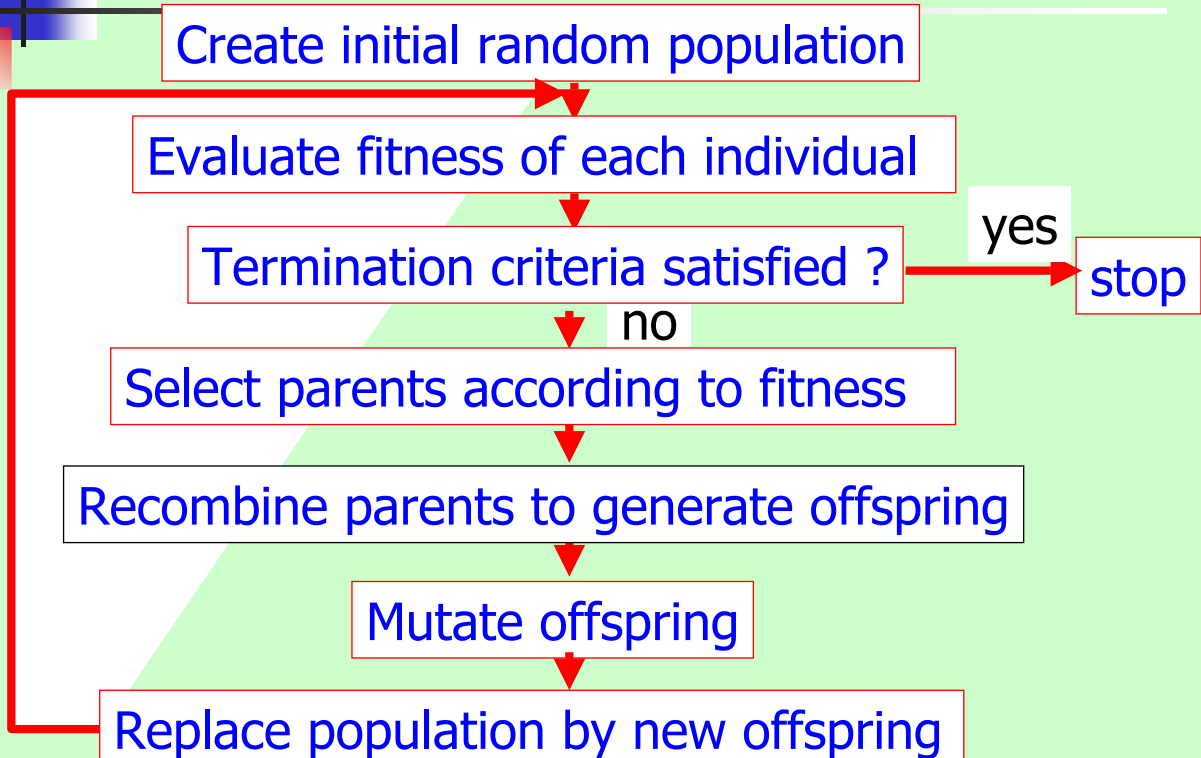
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# Evolutionary Algorithms



# Pseudo Code of an Evolutionary Algorithm



# A Simple Genetic Algorithm

► **Optimization task** : find the maximum of  $f(x)$

for example  $f(x) = x \cdot \sin(x)$   $x \in [0, \pi]$

• **genotype**: binary string  $s \in [0,1]^5$  e.g. 11010, 01011, 10001

• mapping : **genotype**  $\rightarrow$  **phenotype**  $n=5$

binary integer encoding:  $x = \pi \cdot \sum_{i=1}^n s_i \cdot 2^{n-i-1} / (2^n - 1)$

## Initial population

genotype	integ.	phenotype	fitness	prop. fitness
11010	26	2.6349	1.2787	30%
01011	11	1.1148	1.0008	24%
10001	17	1.7228	1.7029	40%
00101	5	0.5067	0.2459	6%

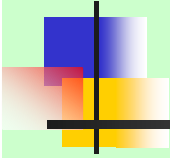
# Some Other Issues Regarding Evolutionary Computing

- **Evolution according to Lamarck.**
  - Individual adapts during lifetime.
  - Adaptations inherited by children.
  - In nature, genes don't change; but for computations we could allow this...
- **Baldwin effect.**
  - Individual's ability to learn has positive effect on evolution.
    - It supports a more diverse gene pool.
    - Thus, more "experimentation" with genes possible.
- **Bacteria and virus.**
  - New evolutionary computing strategies.



# Lecture 7

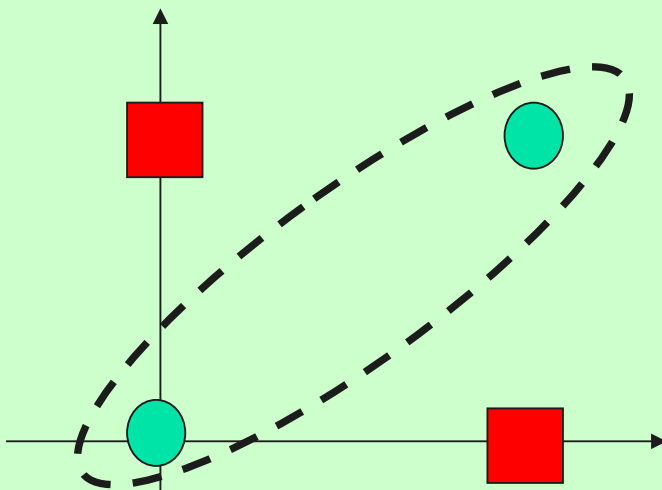
## Radial Basis Functions



## Radial Basis Functions

## Radial-basis function (RBF) networks

**RBF = radial-basis function: a function which depends only on the radial distance from a point**



XOR problem

*quadratically separable*

# Radial-basis function (RBF) networks

So RBFs are functions taking the form

$$\phi (\| \underline{x} - \underline{x}_i \|)$$

where  $\phi$  is a nonlinear activation function,  $\underline{x}$  is the input and  $\underline{x}_i$  is the  $i$ 'th position, prototype, *basis or centre vector*.

The idea is that points near the centres will have similar outputs (i.e. if  $\underline{x} \sim \underline{x}_i$  then  $f(\underline{x}) \sim f(\underline{x}_i)$ ) since they should have similar properties.

The simplest is the linear RBF :  $\phi(\underline{x}) = \|\underline{x} - \underline{x}_i\|$

## Typical RBFs include

(a) **Multiquadrics**

$$\phi (r) = (r^2 + c^2)^{1/2}$$

for some  $c > 0$

(b) **Inverse multiquadrics**

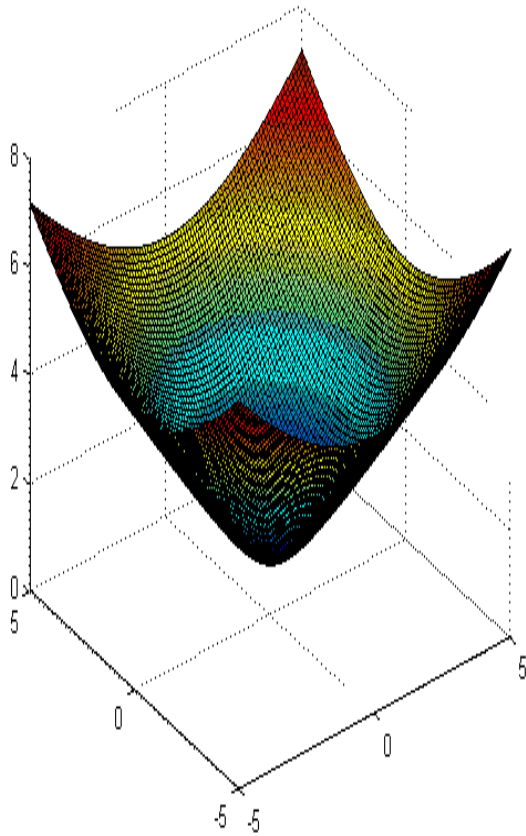
$$\phi (r) = (r^2 + c^2)^{-1/2}$$

for some  $c > 0$

(c) **Gaussian**

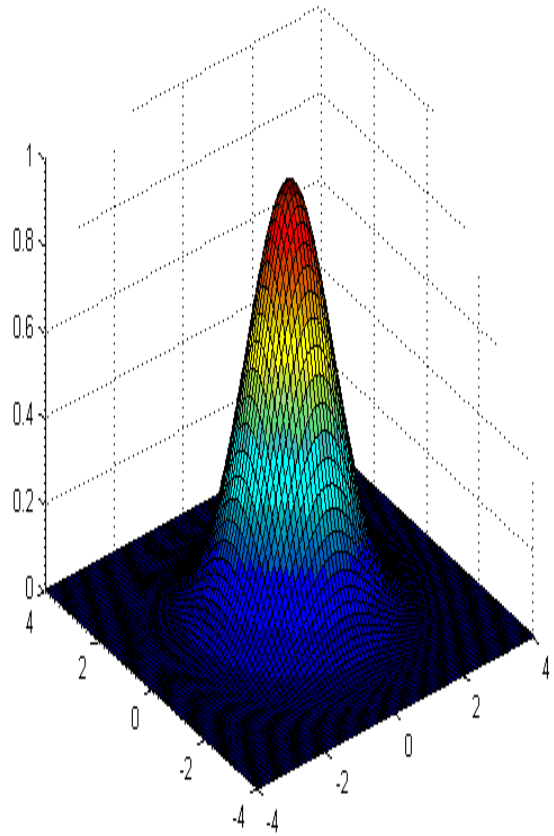
$$\phi(r) = \exp\left(-\frac{r^2}{2\sigma^2}\right)$$

for some  $\sigma > 0$



**'nonlocalized' functions**

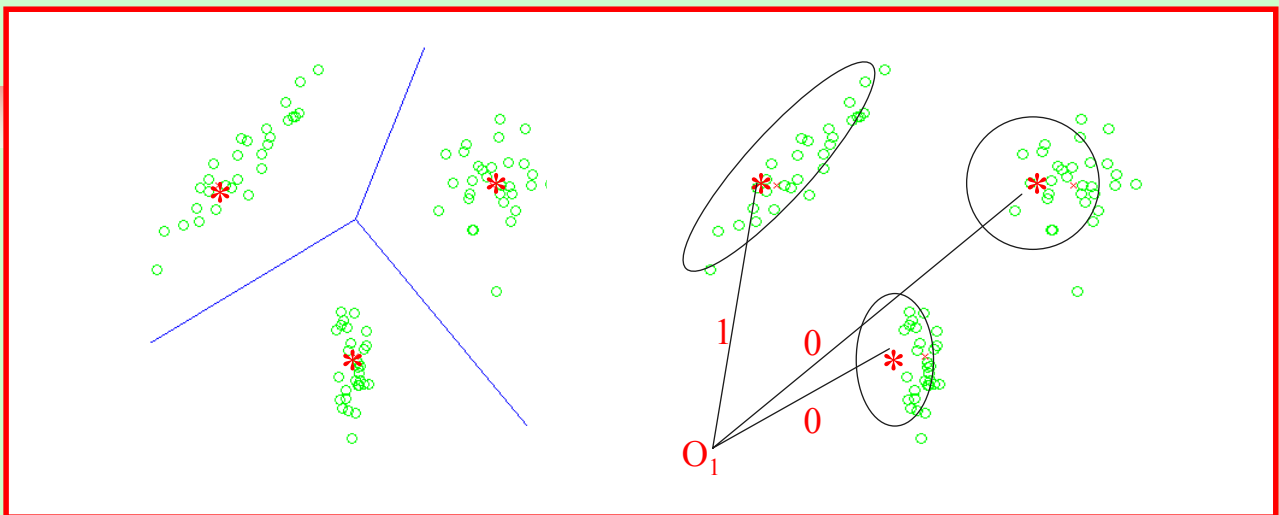
17/03/2008



**'localized' functions**

17/03/2008

- Idea is to use a weighted sum of the outputs from the basis functions to represent the data.
- Thus centers can be thought of as prototypes of input data.



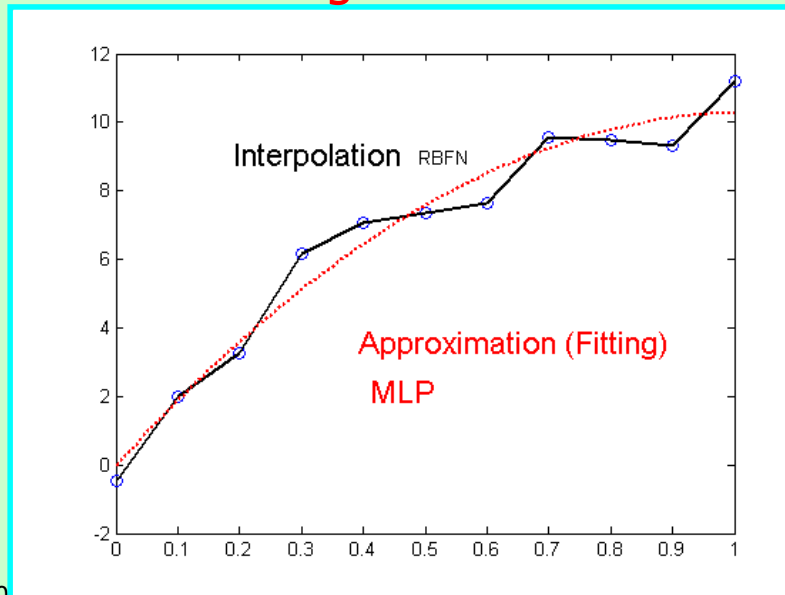
**MLP**  
distributed

vs

**RBF**  
local

## Starting point: exact interpolation

Each input pattern  $x$  must be mapped onto a target value  $d$



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That is, given a set of  $N$  vectors  $\underline{x}_i$  and a corresponding set of  $N$  real numbers,  $d_i$  (the targets), find a function  $F$  that satisfies the interpolation condition:

$$F(\underline{x}_i) = d_i \quad \text{for } i = 1, \dots, N$$

or more exactly find:

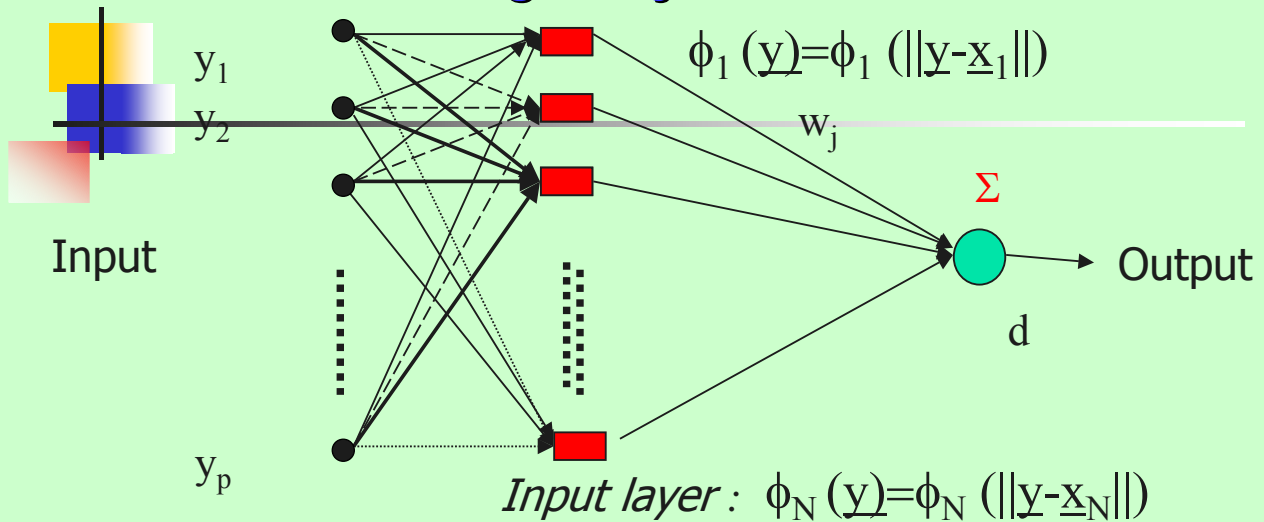
$$F(\underline{x}) = \sum_{j=1}^N w_j \phi(\|\underline{x} - \underline{x}_j\|)$$

satisfying:

$$F(\underline{x}_i) = \sum_{j=1}^N w_j \phi(\|\underline{x}_i - \underline{x}_j\|) = d_i$$

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- output =  $\sum w_i \phi_i(\underline{y} - \underline{x}_i)$
- adjustable parameters are weights  $w_j$
- number of **input units**  $\leq$  number of data points
- Form of the basis functions decided in advance

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## To summarize:

For a given data set containing  $N$  points  $(\underline{x}_i, d_i)$ ,  $i=1, \dots, N$

- ❖ Choose a RBF function  $\phi$
- ❖ Calculate  $\phi(\underline{x}_j - \underline{x}_i)$
- ❖ Solve the linear equation  $\Phi \underline{W} = \underline{D}$
- ❖ Get the unique solution
- ❖ Done

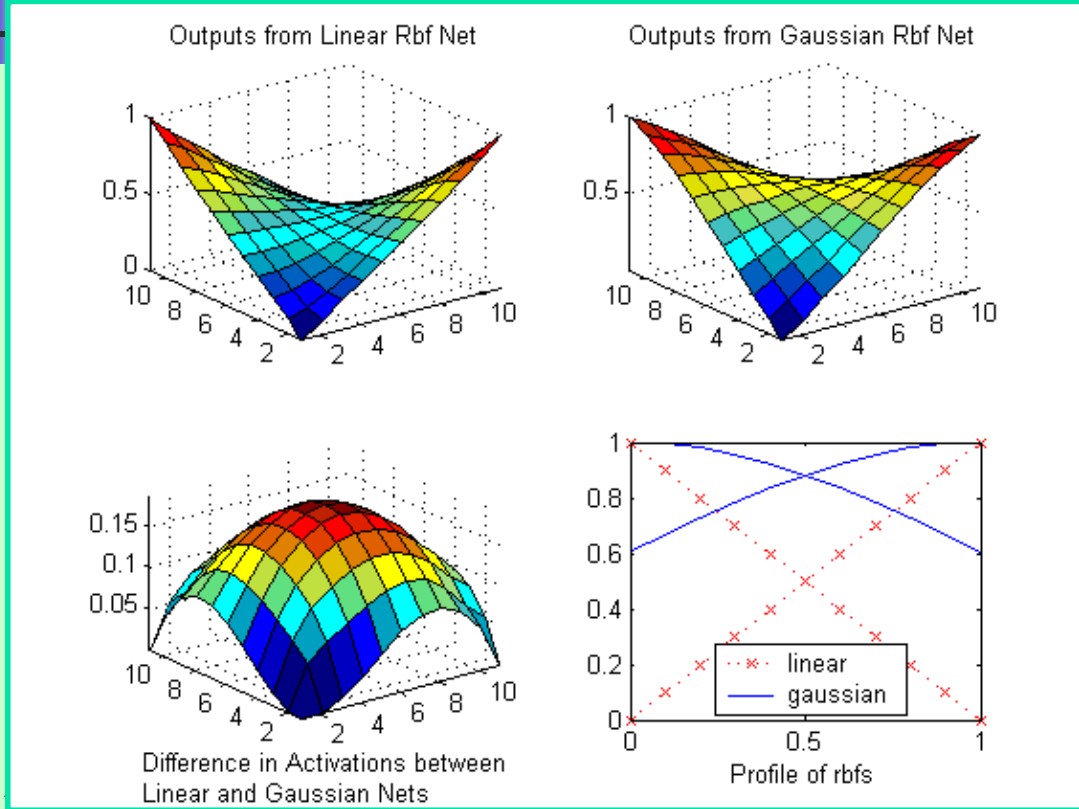
➤ Like MLP's, RBFNs can be shown to be able to approximate any function to arbitrary accuracy (using an arbitrarily large numbers of basis functions).

➤ Unlike MLP's, however, they have the property of 'best approximation' i.e. there exists an RBFN with minimum approximation error.

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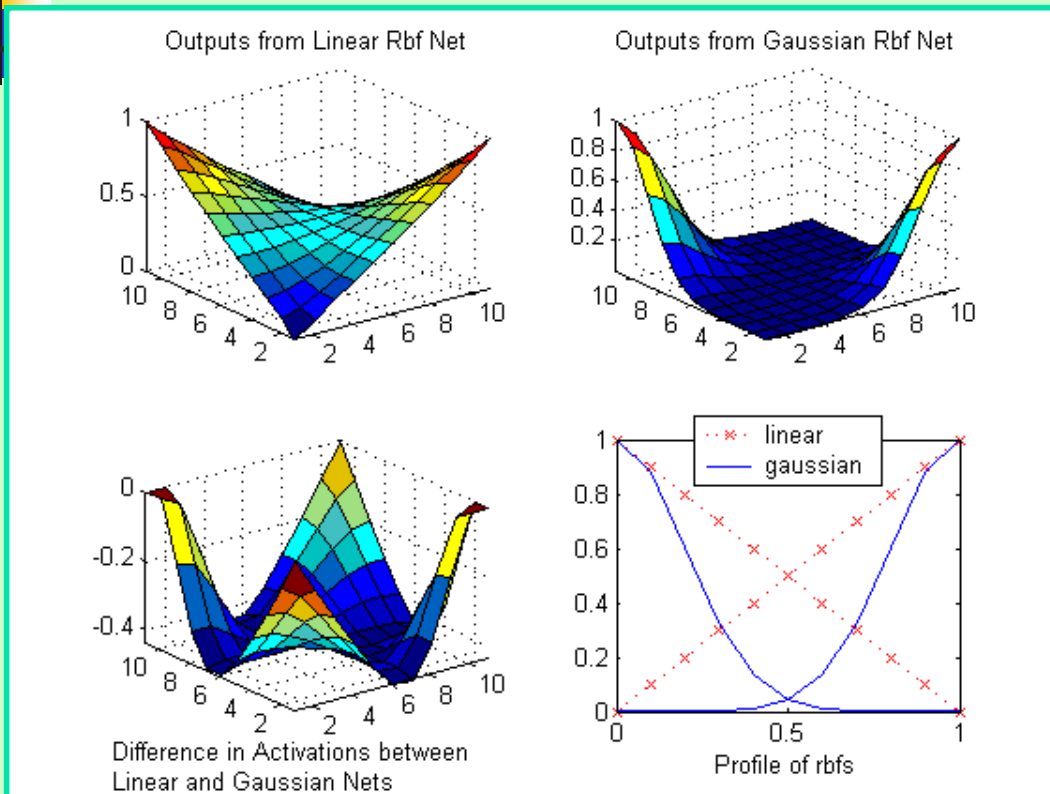
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# Large $\sigma = 1$



7

# Small $\sigma = 0.2$



# Problems with exact interpolation

can produce poor generalisation performance as only data points constrain mapping

## Overfitting problem

*Bishop(1995) example*

Underlying function  $f(x)=0.5+0.4\text{sine}(2\pi x)$   
sampled randomly for 30 points

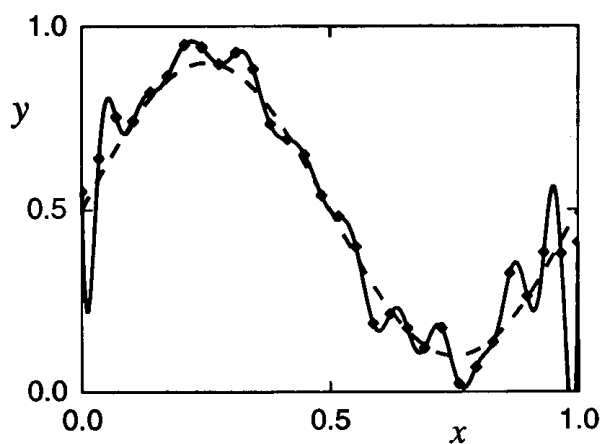
added Gaussian noise to each data point

30 data points 30 hidden RBF units

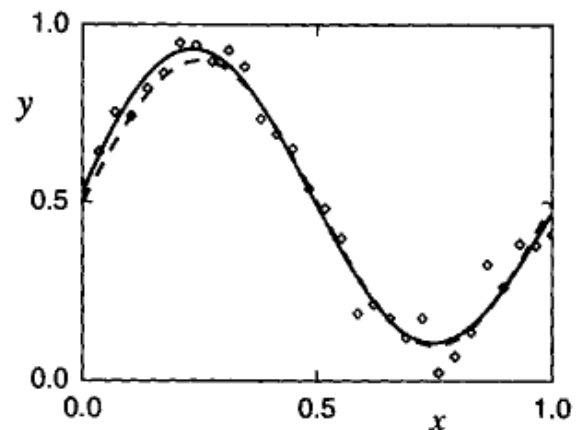
fits all data points but creates oscillations due added noise  
and unconstrained between data points

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All Data Points



5 Basis functions

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**To fit an RBF to every data point is very inefficient due to the computational cost of matrix inversion and is very bad for generalization so:**

- ✓ Use less RBF's than data points I.e.  $M < N$
- ✓ Therefore don't necessarily have RBFs centred at data points
- ✓ Can include bias terms
- ✓ Can have Gaussian with general covariance matrices but there is a trade-off between complexity and the number of parameters to be found eg for  $d$  rbfs we have:

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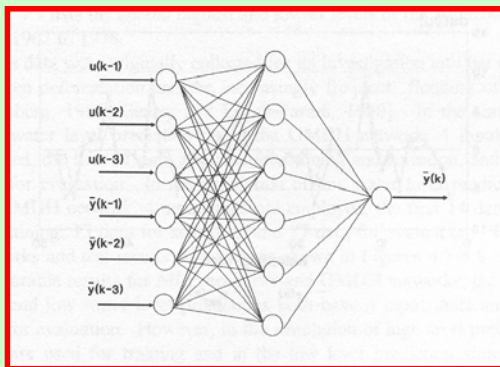
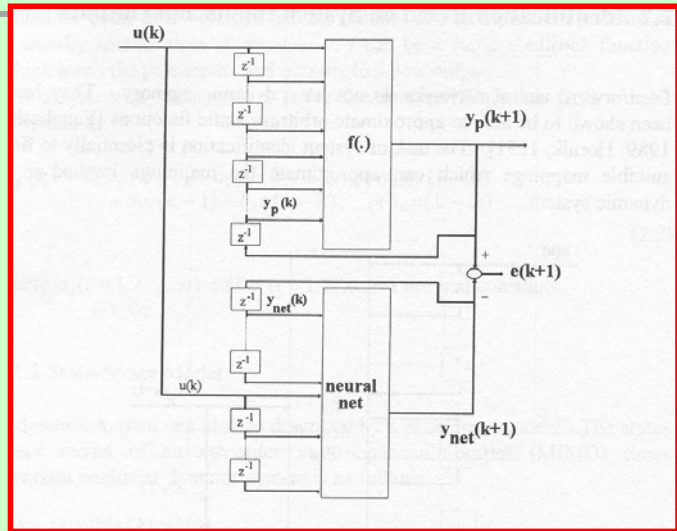
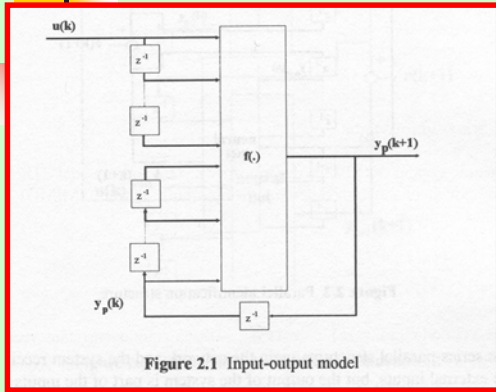
## Application Examples

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**Lecture 9:  
Nonlinear Identification, Prediction  
and Control**

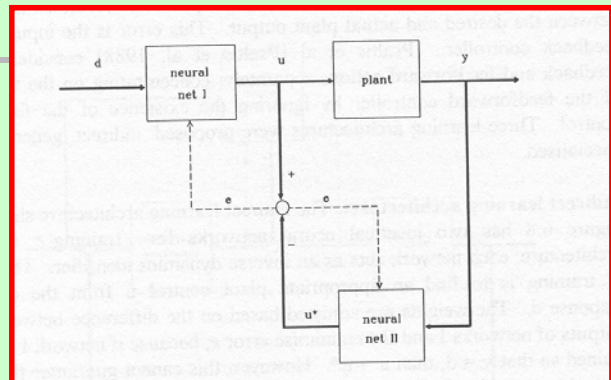
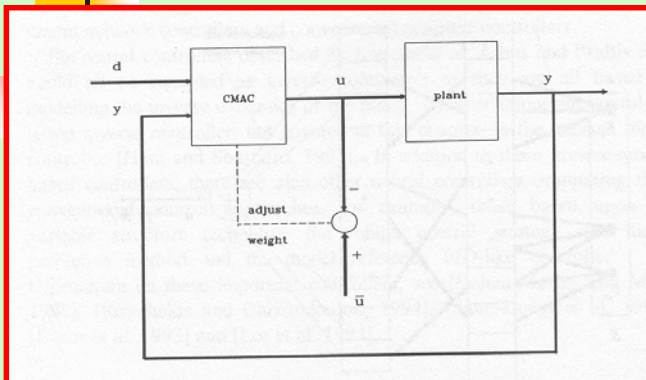


# Nonlinear System Identification



Target function:  $y_p(k+1) = f(.)$   
 Identified function:  $y_{NET}(k+1) = F(.)$   
 Estimation error:  $e(k+1)$

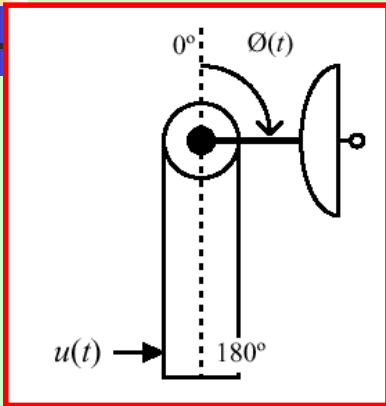
# Nonlinear System Neural Control



d: reference/desired response  
 y: system output/desired output  
 u: system input/controller output  
 $\hat{u}$ : desired controller input  
 $u^*$ : NN output  
 e: controller/network error

The goal of training is to find an appropriate plant control  $u$  from the desired response  $d$ . The weights are adjusted based on the difference between the outputs of the networks I & II to minimise  $e$ . If network I is trained so that  $y = d$ , then  $u = u^*$ . Networks act as inverse dynamics identifiers.

# Nonlinear System Identification



$$\frac{d}{dt} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} x_2 \\ 9.81 \sin x_1 - 2x_2 + u \end{bmatrix}$$

$x_1 = \vartheta$   
 $x_2 = \frac{d\vartheta}{dt}$

```
deg2rad = pi/180;
angle = [-20:40:200]*deg2rad;
vel = [-90:36:90]*deg2rad;
force = -30:6:30;
```

```
angle2 = [-20:10:200]*deg2rad;
Pm = [combvec(angle,vel,force);
      [angle2; zeros(2,length(angle2))]];
```

Neural network  
input generation  
Pm

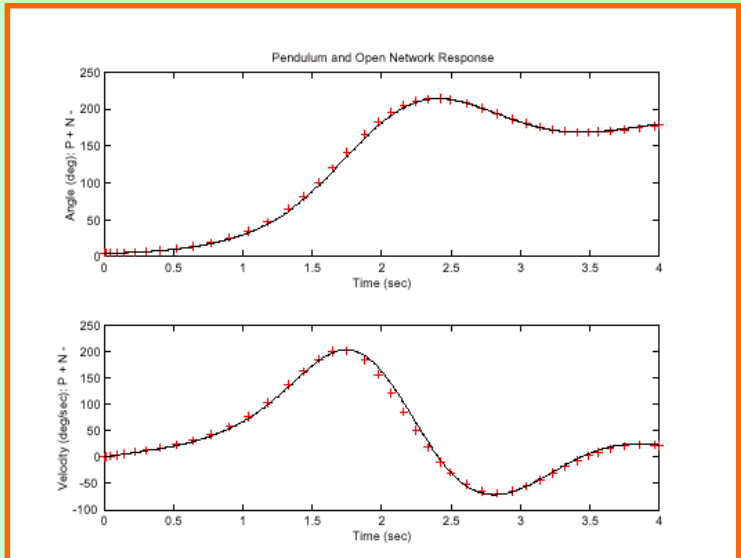
# Nonlinear System Identification

```
S1 = 8;
[S2,Q] = size(Tm);
mnet = newff(minmax(Pm),[S1 S2],{'tansig' 'purelin'},'trainlm');
```

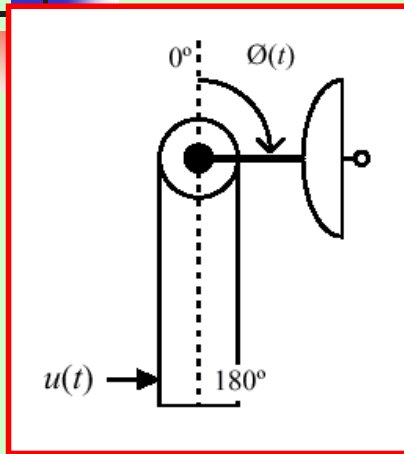
```
mnet.trainParam.goal = (0.0037^2);
mnet = train(mnet,Pm,Tm);
```

Neural network target  
Tm

Neural network response  
(angle & velocity)



# Model Reference Control



$$\frac{d}{dt} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} x_2 \\ 9.81 \sin x_1 - 2x_2 + u \end{bmatrix}$$

$$x_1 = \varnothing$$

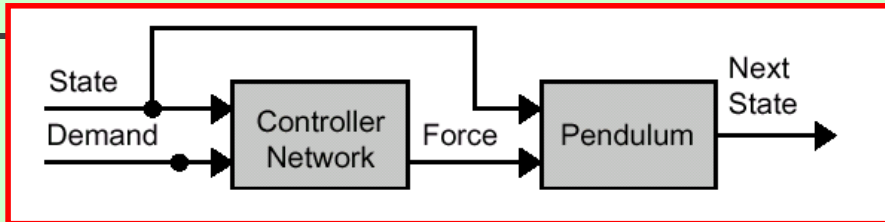
$$x_2 = \frac{d\varnothing}{dt}$$

**Antenna arm nonlinear model**

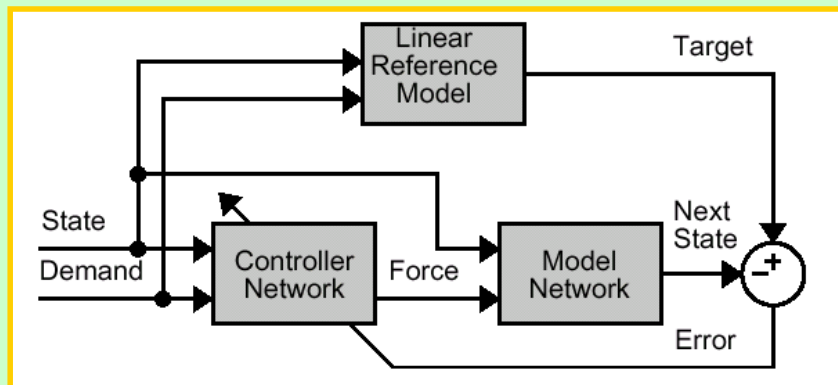
**Linear reference model**

$$\frac{d}{dt} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} x_2 \\ -9x_1 - 6x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 9r \end{bmatrix}$$

# Model Reference Control

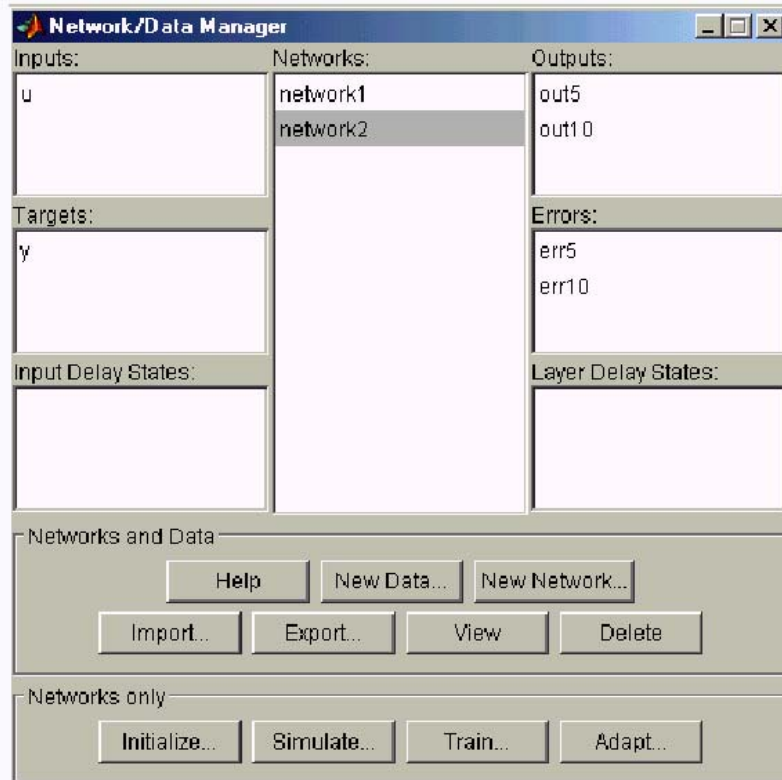


**Neural controller + nonlinear system diagram**

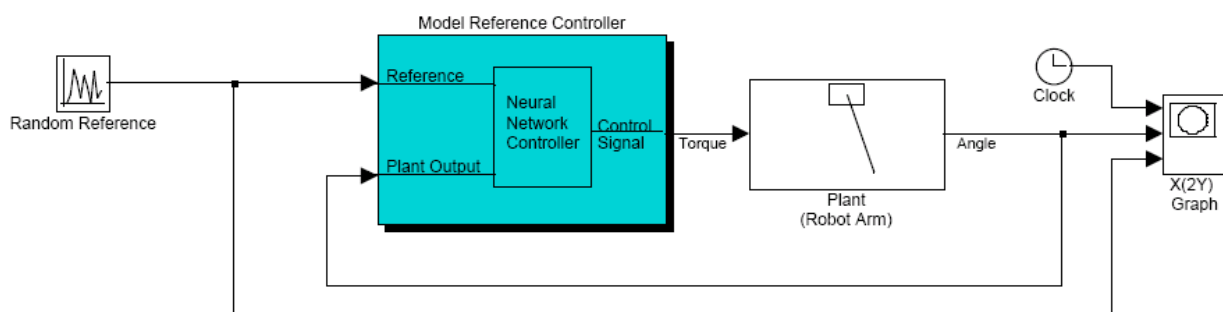


**Neural controller, reference model, neural model**

# Matlab NNtool GUI (Graphical User Interface)



## Control of a Robot Arm Example



Neural Network Model Reference Control of a Robot Arm  
(Double click on the "?" for more info)



Double click  
here for  
Simulink Help

To start and stop the simulation, use the "Start/Stop"  
selection in the "Simulation" pull-down menu

# Control of a Robot Arm Example

**Model Reference Control**

File Window Help

**Network Architecture**

- Size of Hidden Layer: 13
- No. Delayed Reference Inputs: 2
- Sampling Interval (sec): 0.05
- No. Delayed Controller Outputs: 1
- Normalize Training Data
- No. Delayed Plant Outputs: 2

**Training Data**

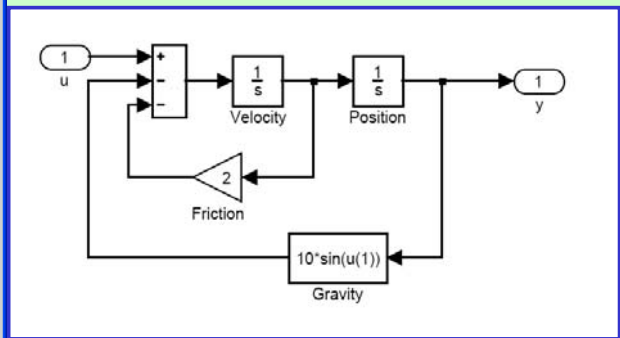
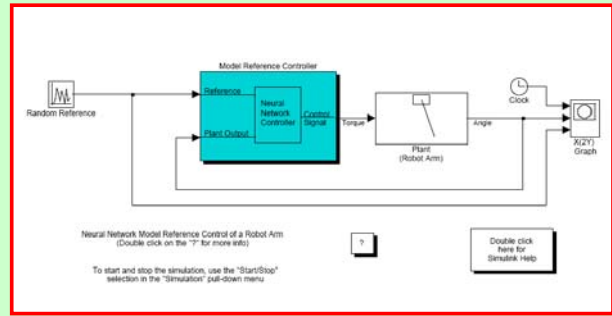
- Maximum Reference Value: 0.7
- Controller Training Samples: 6000
- Minimum Reference Value: -0.7
- Maximum Interval Value (sec): 2
- Reference Model: Browse
- Minimum Interval Value (sec): 0.1
- robotref

**Training Parameters**

- Controller Training Epochs: 10
- Controller Training Segments: 30
- Use Current Weights
- Use Cumulative Training

Buttons: Plant Identification, Train Controller, OK, Cancel, Apply

Perform plant identification before controller training.



# Control of a Robot Arm Example

**Plant Identification**

File Window Help

**Network Architecture**

- Size of Hidden Layer: 10
- No. Delayed Plant Inputs: 2
- Sampling Interval (sec): 0.05
- No. Delayed Plant Outputs: 2
- Normalize Training Data

**Training Data**

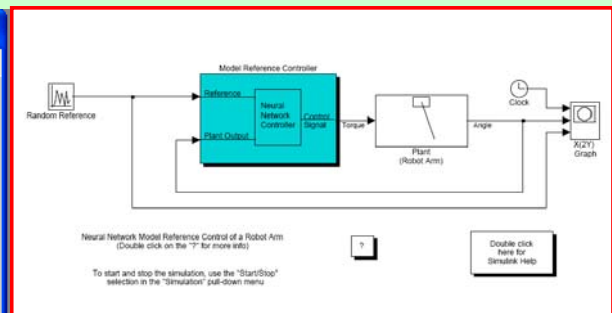
- Training Samples: 10000
- Limit Output Data
- Maximum Plant Input: 15
- Maximum Plant Output: 3.1
- Minimum Plant Input: -15
- Minimum Plant Output: -3.1
- Maximum Interval Value (sec): 2
- Simulink Plant Model: Browse
- Minimum Interval Value (sec): 0.1
- robotarm

**Training Parameters**

- Training Epochs: 300
- Training Function: trainlm
- Use Current Weights
- Use Validation Data
- Use Testing Data

Buttons: Train Network, OK, Cancel, Apply

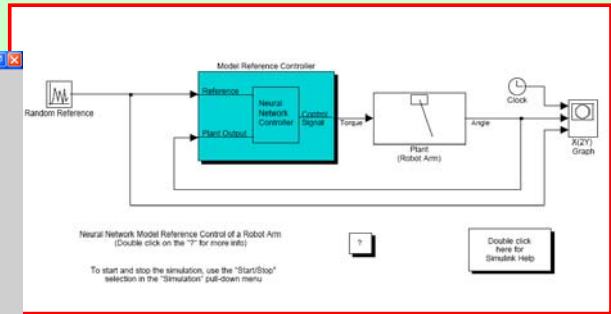
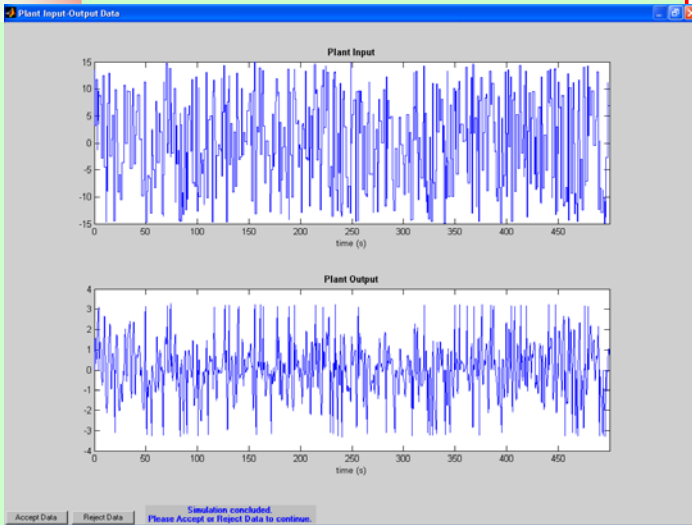
Generate or import data before training the neural network plant.



## Plant Identification:

Data generation from the Reference Model for Neural Network training

# Control of a Robot Arm Example



## After Plant Identification:

### Neural Network training

# Control of a Robot Arm Example

**Plant Identification**

File Window Help

**Plant Identification**

Network Architecture

Size of Hidden Layer: 10    No. Delayed Plant Inputs: 2

Sampling Interval (sec): 0.05    No. Delayed Plant Outputs: 2

Normalize Training Data

Training Data

Training Samples: 10000     Limit Output Data

Maximum Plant Input: 15    Maximum Plant Output: 3.1

Minimum Plant Input: -15    Minimum Plant Output: -3.1

Maximum Interval Value (sec): 2    Simulink Plant Model: Browse

Minimum Interval Value (sec): 0.1    robotarm

Erase Generated Data    Import Data    Export Data

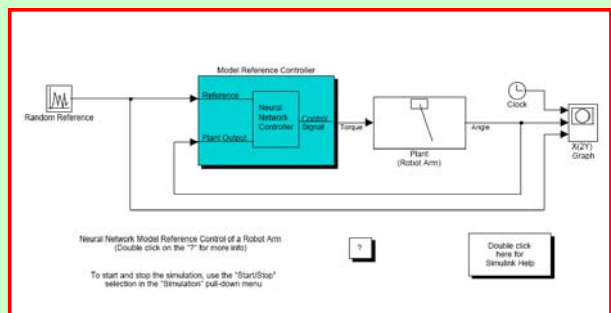
Training Parameters

Training Epochs: 300    Training Function: trainlm

Use Current Weights     Use Validation Data     Use Testing Data

Train Network    OK    Cancel    Apply

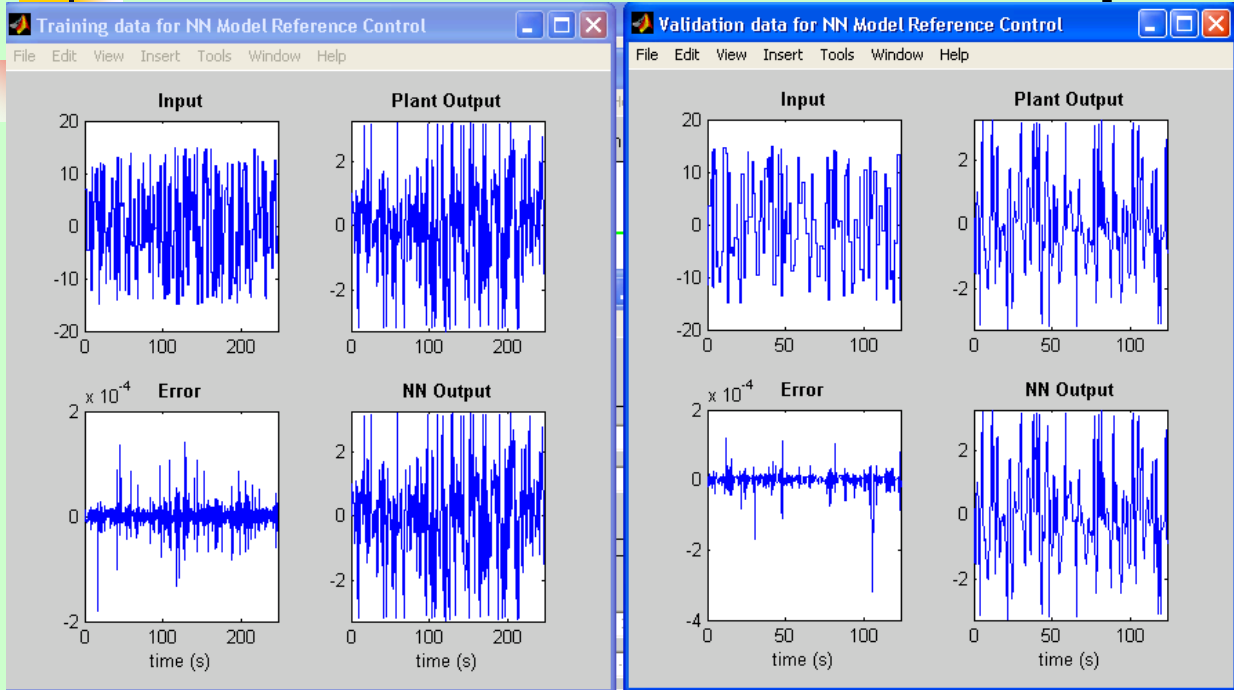
Your training data set has 10000 samples.  
You can now train the network.



## After Plant Identification:

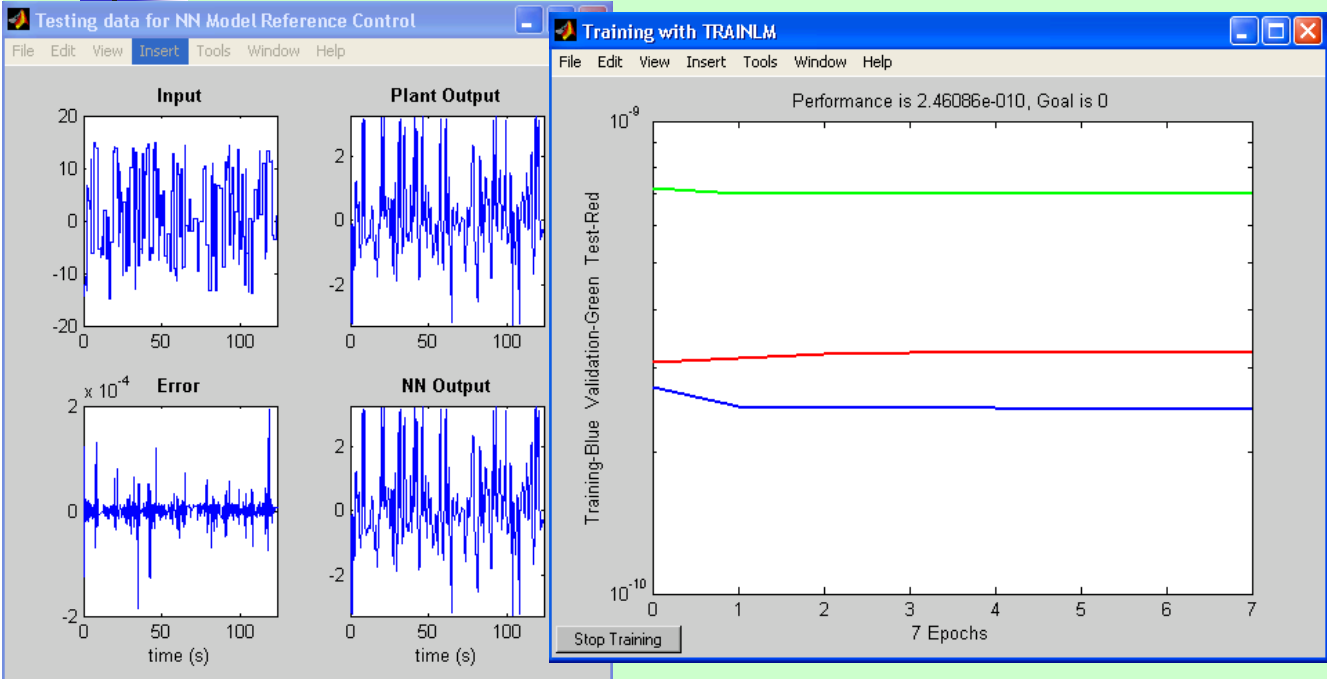
### Neural Network training

# Control of a Robot Arm Example



## Training and Validation Data

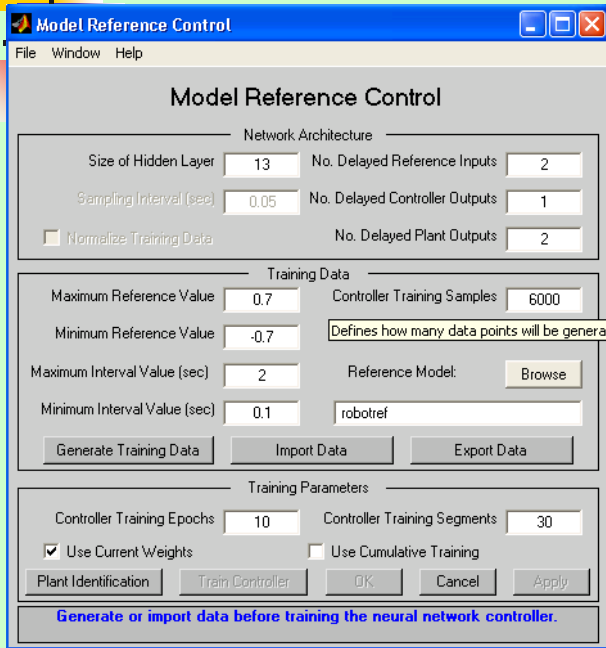
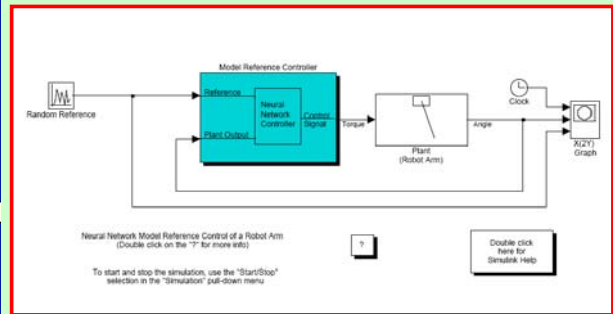
# Control of a Robot Arm Example



## Testing Data and Training Results



# Control of a Robot Arm Example

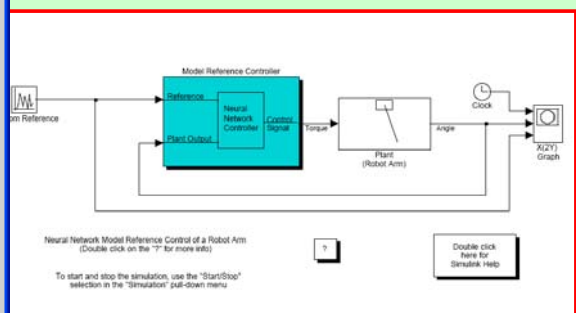
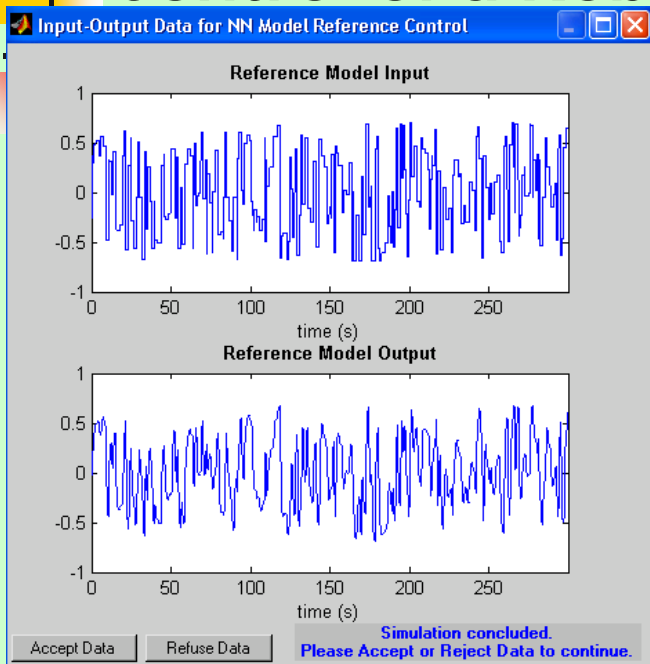



## Plant identification with a NN Data Generation for NN Controller Identification

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# Control of a Robot Arm Example



## Accept the Data Generated for NN Controller Identification

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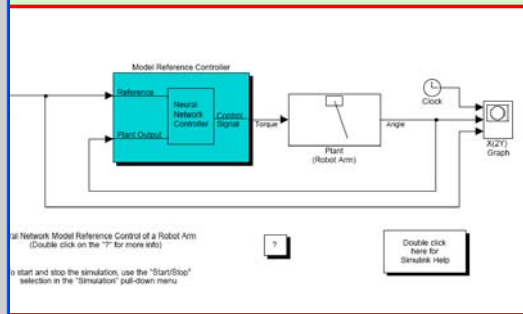
# Control of a Robot Arm Example

The screenshot shows the 'Model Reference Control' window with the following settings:

- Network Architecture:** Size of Hidden Layer: 13, No. Delayed Reference Inputs: 2, Sampling Interval (sec): 0.05, No. Delayed Controller Outputs: 1, No. Delayed Plant Outputs: 2.  Normalize Training Data.
- Training Data:** Maximum Reference Value: 0.7, Minimum Reference Value: -0.7, Maximum Interval Value (sec): 2, Minimum Interval Value (sec): 0.1, Controller Training Samples: 6000, Reference Model: robotref.
- Training Parameters:** Controller Training Epochs: 10, Controller Training Segments: 30,  Use Current Weights,  Use Cumulative Training.

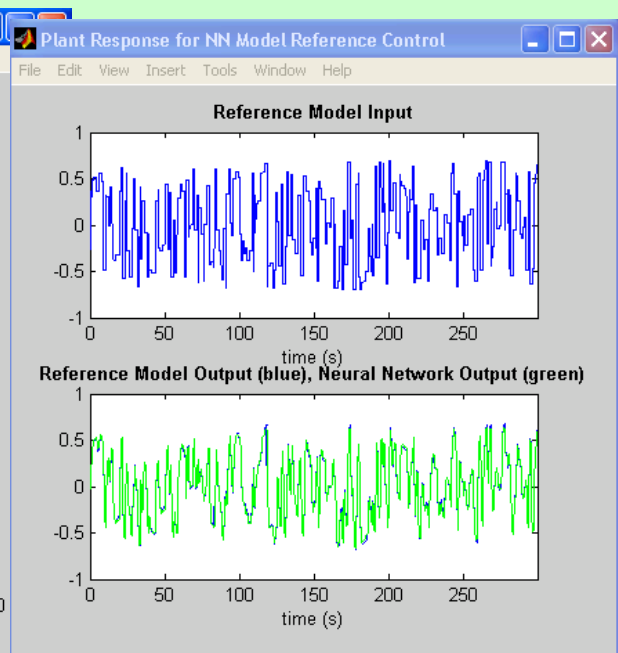
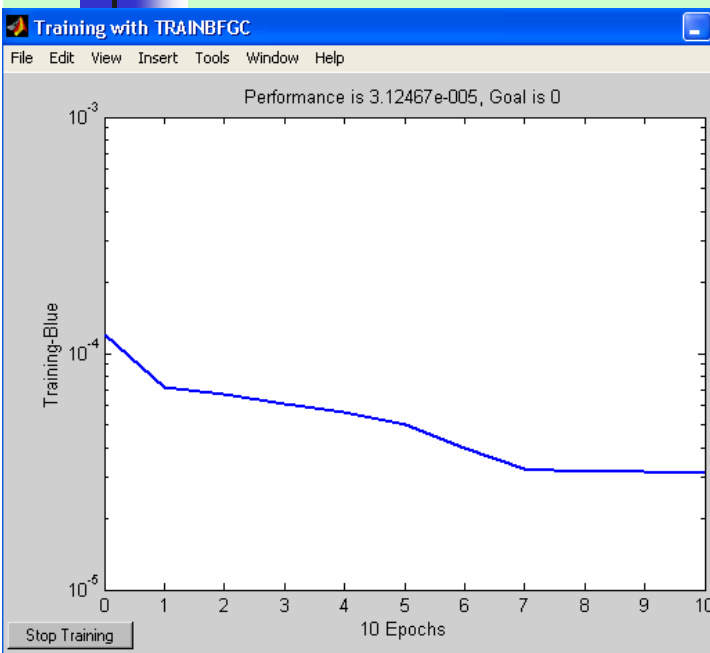
Buttons: Erase Generated Data, Import Data, Export Data, Plant Identification, Train Controller, OK, Cancel, Apply.

Message: Your training data set has 6000 samples. You can now train the network.



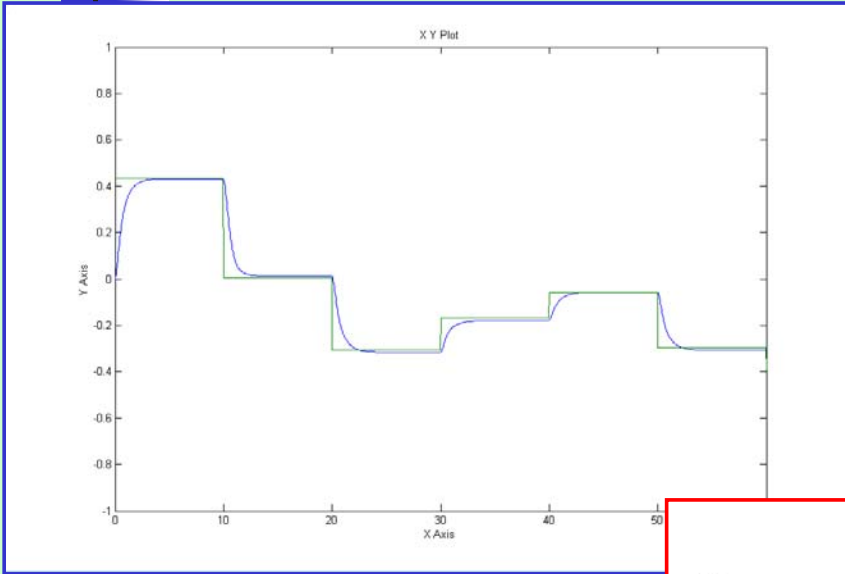
## NN Controller Training

# Control of a Robot Arm Example



## NN Controller Training and Results

# Control of a Robot Arm Example



Reference and Tracked Output Signals

Simulation Final Results

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